Motion of Charged Particle in a Magnetic Field.

If a particle carrying a positive charge q and moving with velocity v enters a magnetic field B then it experiences a force F which is given by the expression

 $F = q(\vec{v} \times \vec{B}) \implies F = qvB\sin\theta$

Here \vec{v} = velocity of the particle, \vec{B} = magnetic field

(1) Zero force

Force on charged particle will be zero (*i.e.* F = 0) if

- (i) No field *i.e.* $B = 0 \Rightarrow F = 0$
- (ii) Neutral particle *i.e.* $q = 0 \Rightarrow F = 0$
- (iii) Rest charge *i.e.* $v = 0 \Rightarrow F = 0$
- (iv) Moving charge *i.e.* $\theta = 0^{\circ}$ or $\theta = 180^{\circ} \Rightarrow F = 0$

(2) **Direction of force**

The force \vec{F} is always perpendicular to both the velocity \vec{v} and the field \vec{B} in accordance with Right Hand Screw Rule, through \vec{v} and \vec{B} themselves may or may not be perpendicular to each other.



Direction of force on charged particle in magnetic field can also be find by Flemings Left Hand Rule (FLHR).

Here, First finger (indicates) \rightarrow Direction of magnetic field

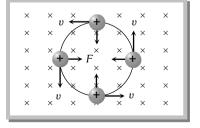
Middle finger \rightarrow Direction of motion of positive charge or direction,

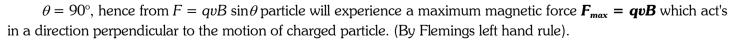
opposite to the motion of negative charge.

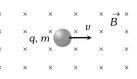
Thumb \rightarrow Direction of force

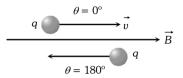
(3) Circular motion of charge in magnetic field

Consider a charged particle of charge q and mass m enters in a uniform magnetic field B with an initial velocity v perpendicular to the field.









(i) **Radius of the path :** In this case path of charged particle is circular and magnetic force provides the necessary centripetal force *i.e.* $qvB = \frac{mv^2}{r} \Rightarrow$ radius of path $r = \frac{mv}{qB}$

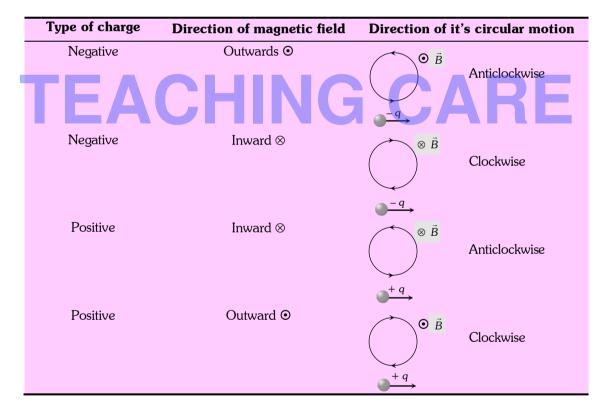
If p = momentum of charged particle and K = kinetic energy of charged particle (gained by charged particle after accelerating through potential difference V) then $p = mv = \sqrt{2mK} = \sqrt{2mqV}$

So $r = \frac{mv}{qB} = \frac{p}{qB} = \frac{\sqrt{2mK}}{qB} = \frac{1}{B}\sqrt{\frac{2mV}{q}}$

 $r \propto v \propto p \propto \sqrt{K}$ *i.e.* with increase in speed or kinetic energy, the radius of the orbit increases.

Note :
$$\cong$$
 Less radius (r) means more curvature (c) i.e. $c \propto \frac{1}{r}$
Less : r More : r $r = \infty$
More : c Less : c $c = 0$

(ii) **Direction of path :** If a charge particle enters perpendicularly in a magnetic field, then direction of path described by it will be



(iii) **Time period** : As in uniform circular motion $v = r\omega$, so the angular frequency of circular motion, called cyclotron or gyro-frequency, will be given by $\omega = \frac{v}{r} = \frac{qB}{m}$ and hence the time period, $T = \frac{2\pi}{\omega} = 2\pi \frac{m}{qB}$

i.e., time period (or frequency) is independent of speed of particle and radius of the orbit and depends only on the field *B* and the nature, *i.e.*, specific charge $\left(\frac{q}{m}\right)$, of the particle.

(4) Motion of charge on helical path

When the charged particle is moving at an angle to the field (other than 0° , 90° , or 180°).

In this situation resolving the velocity of the particle along and perpendicular to the field, we find that the particle moves with constant velocity $v \cos \theta$ along the field (as no force acts on a charged particle when it moves parallel to the field) and at the same time it is also moving with velocity $v \sin \theta$ perpendicular to the field due to

which it will describe a circle (in a plane perpendicular to the field) of radius. $r = \frac{m(vsin\theta)}{r^{P}}$



Time period and frequency do not depend on velocity and so they are given by $T = \frac{2\pi m}{qB}$ and $v = \frac{qB}{2\pi m}$

So the resultant path will be a *helix* with its axis parallel to the field \vec{B} as shown in figure in this situation.

The pitch of the helix, (i.e., linear distance travelled in one rotation) will be given by $p = T(v \cos \theta) = 2\pi \frac{m}{qB}(v \cos \theta)$

Note : ≅

1 rotation = $2\pi = T$ and 1 pitch = 1T

 \cong Number of pitches = Number of rotations = Number of repetition = Number of helical turns

If pitch value is p, then number of pitches obtained in length l given as

Number of pitches =
$$\frac{l}{p}$$
 and time reqd. $t = \frac{l}{v \cos \theta}$

Some standard results

 \cong

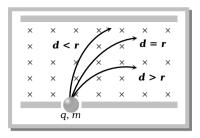
Ratio of radii of path described by proton and α -particle in a magnetic field (particle enters perpendicular to the field)

Constant quantity	Formula	Ratio of radii	Ratio of curvature (c)
v - same	$r = \frac{mv}{qB} \Rightarrow r \propto \frac{m}{q}$	$r_p:r_{\alpha}=1:2$	$c_p : c_R = 2 : 1$
p - same	$r=\frac{p}{qB}\Longrightarrow r\propto\frac{1}{q}$	$r_p:r_{\alpha}=2:1$	$c_p : c_R = 1 : 2$
k - same	$r = rac{\sqrt{2mk}}{qB} \Rightarrow r \propto rac{\sqrt{m}}{q}$	$r_p:r_{\alpha}=1:1$	$c_p : c_R = 1 : 1$
V - same	$r \propto \sqrt{rac{m}{q}}$	$r_p:r_{\alpha}=1:\sqrt{2}$	$c_p:c_R=\sqrt{2}:1$

[•] Particle motion between two parallel plates $(\vec{v} \perp \vec{B})$

- (i) To strike the opposite plate it is essential that d < r.
- (ii) Does not strike the opposite plate d > r.
- (iii) To touch the opposite plate d = r.
- (iv) To just not strike the opposite plate $d \ge r$.
- (v) To just strike the opposite plate $d \le r$.

(5) Lorentz force



When the moving charged particle is subjected simultaneously to both electric field \vec{E} and magnetic field \vec{B} , the moving charged particle will experience electric force $\vec{F}_e = q\vec{E}$ and magnetic force $\vec{F}_m = q(\vec{v} \times \vec{B})$; so the net force on it will be $\vec{F} = q[\vec{E} + (\vec{v} \times \vec{B})]$. Which is the famous 'Lorentz-force equation'.

Depending on the directions of \vec{v}, E and \vec{B} following situations are possible

(i) When \vec{v}, \vec{E} and \vec{B} all the three are collinear : In this situation as the particle is moving parallel or

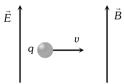
antiparallel to the field, the magnetic force on it will be zero and only electric force will act and so $\vec{a} = \frac{F}{m} = \frac{q\vec{E}}{m}$

The particle will pass through the field following a straight line path (parallel field) with change in its speed. So in this situation speed, velocity, momentum kinetic energy all will change without change in direction of motion as shown

snown

(ii) When \vec{E} is parallel to \vec{B} and both these fields are perpendicular to \vec{v} then : $\vec{F_e}$ is

perpendicular to $\overrightarrow{F_m}$ and they cannot cancel each other. The path of charged particle is curved in both these fields.



(iii) \vec{v}, \vec{E} and \vec{B} are mutually perpendicular : In this situation if \vec{E} and \vec{B} are such that

$$\vec{F} = \vec{F}_e + \vec{F}_m = 0$$
 i.e., $\vec{a} = (\vec{F} / m) = 0$

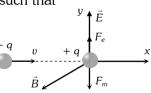
as shown in figure, the particle will pass through the field with same velocity.

And in this situation, as $F_e = F_m$ i.e., qE = qvB v = E/B

This principle is used in 'velocity-selector' to get a charged beam having a specific velocity.

Note : \cong From the above discussion, conclusion is as follows

- \cong If E = 0, B = 0, so F = 0.
- \cong If $E = 0, B \neq 0$, so F may be zero (if $\theta = 0^{\circ}$ or 180°).
- \cong If $E \neq 0$, $B \neq 0$, so F = 0 (if $|\vec{F}_e| = |\vec{F}_m|$ and their directions are opposite)
- \cong If $E \neq 0$, B = 0, so $F \neq 0$ (because $\vec{v} \neq \text{constant}$).



Cyclotron.

Cyclotron is a device used to accelerated positively charged particles (like, α -particles, deutrons etc.) to acquire

enough energy to carry out nuclear disintegration *etc.* t is based on the fact that the electric field accelerates a charged particle and the magnetic field keeps it revolving in circular orbits of constant frequency. Thus a small potential difference would impart if enormously large velocities if the particle is made to traverse the potential difference a number of times.

It consists of two hollow *D*-shaped metallic chambers D_1 and D_2 called dees. The two dees are placed horizontally with a small gap separating them. The dees are connected to the source of high frequency electric field. The dees are enclosed in a metal box containing a gas at a

electric field. The dees are enclosed in a metal box containing a gas at a low pressure of the order of 10^{-3} mm mercury. The whole apparatus is placed between the two poles of a strong electromagnet NS as shown in fig. The magnetic field acts perpendicular to the plane of the dees.

Note : The positive ions are produced in the gap between the two dees by the ionisation of the gas. To produce proton, hydrogen gas is used; while for producing alpha-particles, helium gas is used.

(1) **Cyclotron frequency :** Time taken by ion to describe *q* semicircular path is given by $t = \frac{\pi r}{v} = \frac{\pi m}{qB}$

If T = time period of oscillating electric field then $T = 2t = \frac{2\pi m}{qB}$ the cyclotron frequency $v = \frac{1}{T} = \frac{Bq}{2\pi m}$

(2) **Maximum energy of position :** Maximum energy gained by the charged particle $E_{\text{max}} = \left(\frac{q^2 B^2}{2m}\right)r^2$

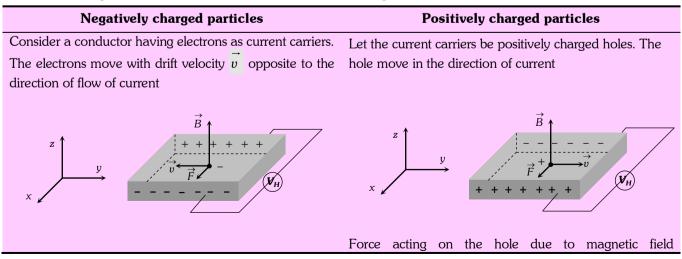
where r_0 = maximum radius of the circular path followed by the positive ion.

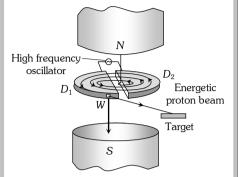
Note : \cong Cyclotron frequency is also known as magnetic resonance frequency.

 \cong Cyclotron can not accelerate electrons because they have very small mass.

Hall effect : The Phenomenon of producing a transverse emf in a current carrying conductor on applying a magnetic field perpendicular to the direction of the current is called Hall effect.

Hall effect helps us to know the nature and number of charge carriers in a conductor.





force acting on electron $F_m = -e(\vec{v} \times \vec{B})$. This force acts $\vec{F_m} = +e(\vec{v} \times \vec{B})$ force acts along x-axis and hence holes along x-axis and hence electrons will move towards face (2) and it becomes positively charged. (2) and it becomes negatively charged.

Concepts The energy of a charged particle moving in a uniform magnetic field does not change because it experiences a force in a ٢ direction, perpendicular to it's direction of motion. Due to which the speed of charged particle remains unchanged and hence it's K.E. remains same. ٢ Magnetic force does no work when the charged particle is displaced while electric force does work in displacing the charged particle. ٢ Magnetic force is velocity dependent, while electric force is independent of the state of rest or motion of the charged particle. If a particle enters a magnetic field normally to the magnetic field, then it starts moving in a circular orbit. The point at which it enters the magnetic field lies on the circumference. (Most of us confuse it with the centre of the orbit) ٢ **Deviation of charged particle in magnetic field :** If a charged particle (q, m) enters a uniform magnetic field B (extends upto a length x) at right angles with speed v as shown in figure. The speed of the particle in magnetic field does not change. But it gets deviated in the magnetic field. Deviation in terms of time t; $\theta = \omega t = \left(\frac{Bq}{m}\right)t$ q, mDeviation in terms of length of the magnetic field; $\theta = \sin^{3}$ This relation can be used only when $x \le r$ For x > r, the deviation will be 180° as shown in the following figure υ x

Example

Example: 28	Electrons move at rig	ght angles to a magnetic fiel	d of $1.5 imes 10^{-2}$ Tesla with	a speed of 6×10^2	27 m/s. If the
	specific charge of the	electron is 1.7×10^{11} Coul/kg	g. The radius of the circula	ar path will be	[BHU 2003]
	(a) 2.9 <i>cm</i>	(b) 3.9 <i>cm</i>	(c) 2.35 <i>cm</i>	(d) 3 <i>cm</i>	
Solution : (c)	$r = \frac{mv}{qB} \implies \frac{v}{(q/m).E}$	$\frac{6 \times 10^{27}}{17 \times 10^{11} \times 1.5 \times 10^{-2}} =$	$2.35 \times 10^{-2} m = 2.35 cm$	1.	
Example: 29	An electron (mass =	9×10^{-31} kg. charge = 1.6 >	$\times 10^{-19}$ coul.) whose kine	tic energy is 7.2×1	.0 ⁻¹⁸ joule is
	moving in a circular o	wrbit in a magnetic field of $9 \times$	$\times 10^{-5}$ weber / m^2 . The rad	lius of the orbit is	[MP PMT 2002]
	(a) 1.25 <i>cm</i>	(b) 2.5 <i>cm</i>	(c) 12.5 <i>cm</i>	(d) 25.0 cm	
Solution : (d)	$r = \frac{\sqrt{2mK}}{qB} = \frac{\sqrt{2 \times q}}{1.6 \times q}$	$\frac{\times 10^{-31} \times 7.2 \times 10^{-8}}{\times 10^{-19} \times q \times 10^{-5}} = 0.25$	cm = 25 cm .		

An electron and a proton enter a magnetic field perpendicularly. Both have same kinetic energy. Which of the

[MP PET 1999]

Example: 30

following is true

(a) Trajectory of electron is less curved (b) Trajectory of proton is less curved (c) Both trajectories are equally curved (d) Both move on straight line path By using $r = \frac{\sqrt{2mk}}{r^{P}}$; For both particles $q \rightarrow$ same, $B \rightarrow$ same, $k \rightarrow$ same Solution : (b) Hence $r \propto \sqrt{m} \implies \frac{r_e}{r_p} = \sqrt{\frac{m_e}{m_p}}$ \therefore $m_p > m_e$ so $r_p > r_e$ Since radius of the path of proton is more, hence it's trajectory is less curved. Example: 31 A proton and an α – particles enters in a uniform magnetic field with same velocity, then ratio of the radii of path describe by them (c) 2:1(a) 1:1 (b) 1:2 (d) None of these By using $r = \frac{mv}{qB}$; $v \to \text{same}$, $B \to \text{same} \implies r \propto \frac{m}{2} \implies \frac{r_p}{r_a} = \frac{m_p}{m_a} \times \frac{q_a}{q_p} = \frac{m_p}{4m_p} \times \frac{2q_p}{q_p} = \frac{1}{2}$ Solution : (b) Example: 32 A proton of mass m and charge +e is moving in a circular orbit of a magnetic field with energy 1MeV. What should be the energy of α -particle (mass = 4 m and charge = +2e), so that it can revolve in the path of same radius [BHU 1997] (a) 1 MeV By using $r = \frac{\sqrt{2mK}}{aB}$; $r \to \text{same}$, $B \to \text{same}$ $\Rightarrow K \propto \frac{q^2}{m}$ Solution : (a) Hence $\frac{K_{\alpha}}{K_{p}} = \left(\frac{q_{\alpha}}{q_{p}}\right)^{2} \times \frac{m_{p}}{m_{p}} = \left(\frac{2q_{p}}{q_{p}}\right)^{2} \times \frac{m_{p}}{4m_{p}} 1 \Rightarrow K_{\alpha} = K_{p} = 1 \text{ meV}.$ A proton and an α – particle enter a uniform magnetic field perpendicularly with the same speed. If proton Example: 33 takes 25μ sec to make 5 revolutions, then the periodic time for the α – particle would be [MP PET 1993] (b) 25 µ sec (a) 50μ sec (c) 10μ sec (d) 5μ sec Time period of proton $T_p = \frac{25}{5} = 5\mu \sec \theta$ Solution : (c) By using $T = \frac{2\pi m}{qB} \implies \frac{T_{\alpha}}{T_p} = \frac{m_{\alpha}}{m_p} \times \frac{q_p}{q_{\alpha}} = \frac{4m_p}{m_p} \times \frac{q_p}{2q_p} \implies T_{\alpha} = 2T_p = 10\mu \text{ sec}.$ A particle with 10^{-11} coulomb of charge and 10^{-7} kg mass is moving with a velocity of 10^8 m/s along the y-axis. Example: 34 A uniform static magnetic field B = 0.5 Tesla is acting along the x-direction. The force on the particle is [MP PMT 1997] (a) $5 \times 10^{-11} N$ along \hat{i} (b) $5 \times 10^3 N$ along \hat{k} (c) $5 \times 10^{-11} N$ along $-\hat{j}$ (d) $5 \times 10^{-4} N$ along $-\hat{k}$ By using $\vec{F} = q(\vec{v} \times \vec{B})$; where $\vec{v} = 10\hat{i}$ and $\vec{B} = 0.5\hat{i}$ Solution : (d) $\Rightarrow \vec{F} = 10^{-11} (10^8 \,\hat{i} \times 0.5 \,\hat{i}) = 5 \times 10^{-4} (\hat{i} \times \hat{i}) = 5 \times 10^{-4} (-\hat{k}) \,i.e., 5 \times 10^{-4} N \,\text{along} - \hat{k}.$

- Example: 35An electron is moving along positive x-axis. To get it moving on an anticlockwise circular path in x-y plane, a
magnetic filed is applied[MP PMT 1999]
 - (a) Along positive y-axis

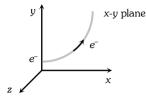
(b) Along positive *z*-axis

(c) Along negative y-axis

- (d) Along negative *z*-axis
- Solution : (a) The given situation can be drawn as follows

According to figure, for deflecting electron in x-y plane, force must be acting an it towards y-axis.

Hence according to Flemings left hand rule, magnetic field directed along positive y – axis.



Example: 36 A particle of charge -16×10^{-18} coulomb moving with velocity 10 m/s along the x-axis enters a region where a magnetic field of induction B is along the y-axis, and an electric field of magnitude 10^4 V/m is along the negative z-axis. If the charged particle continuous moving along the x-axis, the magnitude of B is [AIEEE 2003]

(a)
$$10^{-3} Wb/m^2$$
 (b) $10^3 Wb/m^2$ (c) $10^5 Wb/m^2$ (d) $10^{16} Wb/m^2$

Solution : (b) Particles is moving undeflected in the presence of both electric field as well as magnetic field so it's speed

$$v = \frac{E}{B} \Rightarrow B = \frac{E}{v} = \frac{10^4}{10} = 10^3 Wb/m^2$$
.

Example: 37 A particle of mass *m* and charge *q* moves with a constant velocity *v* along the positive *x* direction. It enters a region containing a uniform magnetic field *B* directed along the negative *z* direction extending from x = a to x = b. The minimum value of *v* required so that the particle can just enter the region x > b is

[IIT-JEE (Screening) 2002]

(a) qbB/m (b) q(b-a)B/m (c) qaB/m

(d) q(b+a)B/2m

Solution : (b) As shown in the following figure, the z-axis points out of the paper and the magnetic fields is directed into the paper, existing in the region between PQ and RS. The particle moves in a circular path of radius r in the magnetic field. It can just enter the region x > b for $r \ge (b-q)$

Now
$$r = \frac{mv}{qb} \ge (b-a)$$

$$\Rightarrow v \ge \frac{q(b-a)B}{m} \Rightarrow v_{\min} = \frac{q(b-a)B}{m}$$

Example: **38** At a certain place magnetic field vertically downwards. An electron approaches horizontally towards you and enters in this magnetic fields. It's trajectory, when seen from above will be a circle which is

- (a) Vertical clockwise (b) Vertical anticlockwise
- (c) Horizontal clockwise (d) Horizontal anticlockwise
- Solution : (c) By using Flemings left hand rule.

Example: **39** When a charged particle circulates in a normal magnetic field, then the area of it's circulation is proportional to

(a) It's kinetic energy

(b) It's momentum

(c) It's charge

(d) Magnetic fields intensity

Υ

 $r = \frac{\sqrt{2mK}}{\alpha R}$ and $A = Aq^2 \Rightarrow A = \frac{\pi(2mK)}{\alpha^2 h^2} \Rightarrow A \propto K.$ Solution : (a)

Example: 40

An electron moves straight inside a charged parallel plate capacitor at uniform charge density σ . The space between the plates is filled with constant magnetic field of induction \vec{B} . Time of straight line motion of the electron in the capacitor is



Solution : (b) The net force acting on the electron is zero because it moves with constant velocity, due to it's motion on straight line.

$$\Rightarrow \vec{F}_{net} = \vec{F}_e + \vec{F}_m = 0 \Rightarrow |\vec{F}_e| = |\vec{F}_m| \Rightarrow eE = evB \Rightarrow ve = \frac{E}{B} = \frac{\sigma}{\varepsilon_0 B} \qquad \begin{bmatrix} E = \frac{\sigma}{\varepsilon_0} \end{bmatrix}$$

$$\therefore \text{ The time of motion inside the capacitor } t = \frac{l}{v} = \frac{\varepsilon_0 lB}{\sigma}.$$

- A proton of mass 1.67×10^{-27} kg and charge 1.6×10^{-19} C is projected with a speed of 2×10^6 m/s at an Example: 41 angle of 60° to the X-axis. If a uniform magnetic field of 0.104 *Tesla* is applied along Y-axis, the path of proton is [IIT-JEE 1995]
 - (a) A circle of radius = 0.2 m and time period $\pi \times 10^{-7}$ s
 - (b) A circle of radius = 0.1 m and time period $2\pi \times 10^{-7}$ s
 - (c) A helix of radius = 0.1 m and time period $2\pi \times 10^{-7}$ s
 - (d) A helix of radius = 0.2 m and time period $4\pi \times 10^{-7}$ s

Solution : (b) By using
$$r = \frac{mv\sin\theta}{qB} \Rightarrow r = \frac{1.67 \times 15^{27} \times 2 \times 10^6 \times \sin 30^\circ}{1.6 \times 10^{-19} \times 0.104} = 0.1m$$

and it's time period $T = \frac{2\pi m}{R} = \frac{2 \times \pi \times 9.1 \times 10^{-31}}{1.6 \times 10^{-19} \times 10^{-31}} = 2\pi \times 10^{-7} \text{ sec}$.

qΒ $1.6 \times 10^{-19} \times 0.104$

Example: 42 A charge particle, having charge q accelerated through a potential difference V enter a perpendicular magnetic field in which it experiences a force F. If V is increased to 5V, the particle will experience a force

(a) *F* (b) 5*F* (c)
$$\frac{F}{5}$$
 (d) $\sqrt{5}F$

 $\frac{1}{2}mv^2 = qV \implies v = \sqrt{\frac{2qV}{m}}$. Also F = qvBSolution : (d)

$$\Rightarrow F = qB\sqrt{\frac{2qV}{m}} \text{ hence } F \propto \sqrt{V} \text{ which gives } F' = \sqrt{5}F.$$

- The magnetic field is downward perpendicular to the plane of the paper and a few charged particles are Example: 43 projected in it. Which of the following is true [CPMT 1997]
 - (a) A represents proton and *B* and electron
 - (b) Both A and B represent protons but velocity of A is more than that of B
 - (c) Both A and B represents protons but velocity of B is more than that of A
 - (d) Both A and B represent electrons, but velocity of B is more than that of A
- Both particles are deflecting in same direction so they must be of same sign. (i.e., both A and B represents protons) Solution : (c)

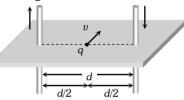
By using
$$r = \frac{mv}{qB} \implies r \propto v$$

From given figure radius of the path described by particle B is more than that of A. Hence $v_B > v_A$.

Two very long straight, particle wires carry steady currents i and -i respectively. The distance between the Example: 44 wires is d. At a certain instant of time, a point charge q is at a point equidistant from the two wires, in the plane of the wires. It's instantaneous velocity \vec{v} is perpendicular to this plane. The magnitude of the force due to the magnetic field acting on the charge at this instant is [IIT-JEE 1998]

(a)
$$\frac{\mu_0 i q v}{2 \pi d}$$
 (b) $\frac{\mu_0 i q v}{\pi d}$ (c) $\frac{2 \mu_0 i q v}{\pi d}$ (d) Zero

Solution : (d) According to gives information following figure can be drawn, which shows that direction of magnetic field is along the direction of motion of charge so net on it is zero.

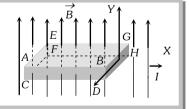


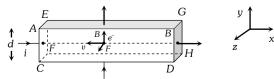
- Example: 45 A metallic block carrying current i is subjected to a uniform magnetic induction B as shown in the figure. The moving charges experience a force F given by which results in the lowering of the potential of the face Assume the speed of the carriers to be v[IIT-JEE 1996]
 - (a) $eVB\hat{k}$, ABCD
 - (b) $eVB\hat{k}$, ABCD
 - eVBk, ABCD (c)
 - (d) $-eVB\hat{k}$. EFGH

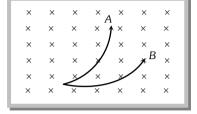


As the block is of metal, the charge carriers are electrons; so for current along positive x-axis, the electrons are moving along negative x-axis, *i.e.* $\vec{v} = -vi$

and as the magnetic field is along the *y*-axis, *i.e.* $\vec{B} = B\hat{j}$ so $\vec{F} = q(\vec{v} \times \vec{B})$ for this case yield $\vec{F} = (-e)[-v\hat{i} \times B\hat{j}]$ i.e., $\vec{F} = evB\hat{k}$ [As $\hat{i} \times \hat{j} = \hat{k}$]





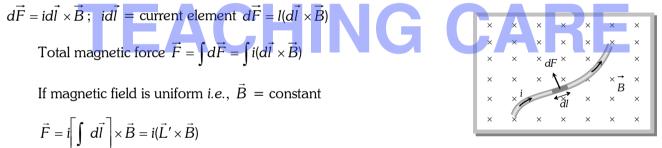


As force on electrons is towards the face ABCD, the electrons will accumulate on it an hence it will acquire lower potential.

Tricky examp	le: 4
	An ionised gas contains both positive and negative ions. If it is subjected simultaneously to an electric field along the $+ve x$ -axis and a magnetic field along the $+z$ direction then [IIT-JEE (Screening) 2000]
	(a) Positive ions deflect towards $+y$ direction and negative ions towards $-y$ direction
	(b) All ions deflect towards $+ y$ direction
	(c) All ions deflect towards $-y$ direction
	(d) Positive ions deflect towards $-y$ direction and negative ions towards $+y$ direction.
Solution : (c)	As the electric field is switched on, positive ion will start to move along positive <i>x</i> -direction and negative ion along negative <i>x</i> -direction. Current associated with motion of both types of ions is along positive <i>x</i> -direction. According to Flemings left hand rule force on both types of ions will be along negative <i>y</i> -direction.

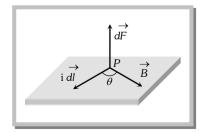
Force on a Current Carrying Conductor in Magnetic Field.

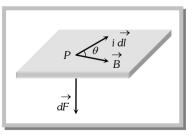
In case of current carrying conductor in a magnetic field force experienced by its small length element is



 $\int d\vec{l} = \vec{L}$ vector sum of all the length elements from initial to final point. Which is in accordance with the law of vector addition is equal to length vector \vec{L}' joining initial to final point.

(1) **Direction of force :** The direction of force is always perpendicular to the plane containing $id\vec{l}$ and \vec{B} and is same as that of cross-product of two vectors $(\vec{A} \times \vec{B})$ with $\vec{A} = id\vec{l}$.





The direction of force when current element $i d\vec{l}$ and \vec{B} are perpendicular to each other can also be determined by applying either of the following rules

Fleming's left-hand ruleRight-hand palm ruleStretch the fore-finger, central finger and thumb left hand
mutually perpendicular. Then if the fore-finger points in the
direction of field \vec{B} and the central in the direction of
current *i*, the thumb will point in the direction of forceStretch the fingers and thumb of right hand at right angles to
each other. Then if the fingers point in the direction of field
 \vec{B} and the central in the direction of force



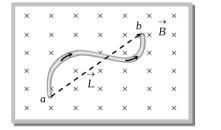
(2) **Force on a straight wire :** If a current carrying straight conductor (length *l*) is placed in an uniform magnetic field (*B*) such that it makes an angle θ with the direction of field then force experienced by it is $F = Bil \sin \theta$

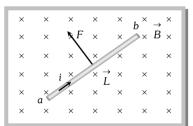
If $\theta = 0^\circ$, F = 0

If $\theta = 90^{\circ}$, $F_{\text{max}} = Bil$

(3) Force on a curved wire

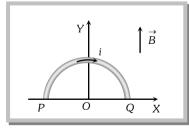
The force acting on a curved wire joining points *a* and *b* as shown in the figure is the same as that on a straight wire joining these points. It is given by the expression $\vec{F} = i\vec{L} \times \vec{B}$



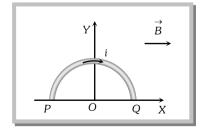


Specific Example

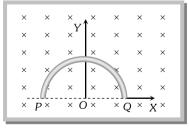
The force experienced by a semicircular wire of radius R when it is carrying a current i and is placed in a uniform magnetic field of induction B as shown.



 $\vec{L}' = 2R\hat{i}$ and $\vec{B} = B\hat{i}$ So by using $\vec{F} = i(\vec{L}' \times \vec{B})$ force on the wire $\vec{F} = i(2R)(B)(\hat{i} \times \hat{i}) \Rightarrow \vec{F} = 0$



 $\vec{L}' = 2R\hat{i}$ and $\vec{B} = B\hat{j}$ $\vec{F} = i \times 2BR(\hat{i} \times \hat{j})$ $\vec{F} = 2BiR\hat{k}$ *i.e.* F = 2BiR(perpendicular to paper outward)



 $\vec{L}' = 2R\hat{i}$ and $\vec{B} = B(-\hat{k})$ $\therefore \vec{F} = i \times 2BR(+\hat{j})$ F = 2BiR (along Y-axis)

12

Force Between Two Parallel Current Carrying Conductors.

When two long straight conductors carrying currents i_1 and i_2 placed parallel to each other at a distance 'a' from each other. A mutual force act between them when is given as

$$F_1 = F_2 = F = \frac{\mu_0}{4\pi} \cdot \frac{2i_1i_2}{a} \times l$$

 $i_1 \uparrow i_2$ $\leftarrow a \rightarrow$ where l is the length of that portion of the conductor on which force is to be calculated.

Hence force per unit length
$$\frac{F}{l} = \frac{\mu_0}{4\pi} \cdot \frac{2i_1i_2}{a} \frac{N}{m}$$
 or $\frac{F}{l} = \frac{2i_1i_2}{a} \frac{dyne}{cm}$

Direction of force: If conductors carries current in same direction, then force between them will be attractive. If conductor carries current in opposite direction, then force between them will be repulsive.

 $M_{ote} \simeq \text{If } a = 1m \text{ and in free space } \frac{F}{I} = 2 \times 10^{-7} N/m \text{ then } i_1 = i_2 = 1Amp \text{ in each identical wire. By this}$ concept S.I. unit of Ampere is defined. This is known as Ampere's law.

Force Between Two Moving Charges.

If two charges q_1 and q_2 are moving with velocities v_1 and v_2 respectively and at any instant the distance between them is r, then

$$\vec{F}_{e} \xleftarrow{q_{1}} \vec{F}_{e} \xleftarrow{q_{2}} \vec{F}_{e} \xrightarrow{\vec{F}_{e}} \vec{F}_{e} \xrightarrow{\vec{F}_{e}} \vec{F}_{e} \xrightarrow{\vec{F}_{e}} \vec{F}_{e} \xleftarrow{q_{1}} \vec{F}_{m} \xrightarrow{\vec{F}_{m}} \vec{F}_{m} \xrightarrow{v_{2}} \vec{F}_{e}$$

Magnetic force between them is
$$F_m = \frac{\mu_0}{4\pi} \cdot \frac{q_1 q_2 v_1 v_2}{r^2}$$
 (i)

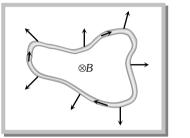
and Electric force between them is $F_e = \frac{1}{4\pi\varepsilon_0} \cdot \frac{q_1q_2}{r^2}$ (ii)

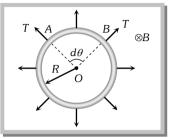
From equation (i) and (ii) $\frac{F_m}{F_e} = \mu_0 \varepsilon_0 v^2$ but $\mu_0 \varepsilon_0 = \frac{1}{c^2}$; where *c* is the velocity light in vacuum. So $\frac{F_m}{F_e} = \left(\frac{v}{c}\right)^2$

If $v \ll c$ then $F_m \ll F_e$

Standard Cases for Force on Current Carrying Conductors.

Case 1: When an arbitrary current carrying loop placed in a magnetic field (\perp to the plane of loop), each element of loop experiences a magnetic force due to which loop stretches and open into circular loop and tension developed in it's each part.





dF

Specific example

In the above circular loop tension in part A and B.

In balanced condition of small part AB of the loop is shown below



Note : ≅If no magnetic field is present, the loop will still open into a circle as in it's adjacent parts current will be in opposite direction and opposite currents repel each other.



Case 2 : Equilibrium of a current carrying conductor : When a finite length current carrying wire is kept parallel to another infinite length current carrying wire, it can suspend freely in air as shown below

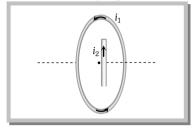


In both the situations for equilibrium of XY it's downward weight = upward magnetic force *i.e.* $mg = \frac{\mu_0}{4\pi} \cdot \frac{2i_1i_2}{h} \cdot l$

Note : \cong In the first case if wire XY is slightly displaced from its equilibrium position, it executes SHM and it's time period is given by $T = 2\pi \sqrt{\frac{h}{g}}$.

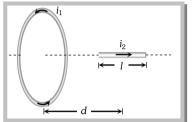
 \cong If direction of current in movable wire is reversed then it's instantaneous acceleration produced is $2g\downarrow$.

Case 3 : Current carrying wire and circular loop : If a current carrying straight wire is placed in the magnetic field of current carrying circular loop.



Wire is placed in the perpendicular magnetic field due to coil at it's centre, so it will experience a

maximum force $F = Bil = \frac{\mu_0 i_1}{2r} \times i_2 l$



wire is placed along the axis of coil so magnetic field produced by the coil is parallel to the wire. Hence it will not experience any force.

Case 4 : Current carrying spring : If current is passed through a spring, then it will contract because current will flow through all the turns in the same direction.

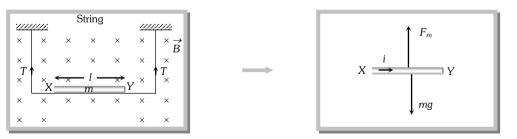


If current makes to flow through spring, then spring will contract and weight lift up

If switch is closed then current start flowing, spring will execute oscillation in vertical plane

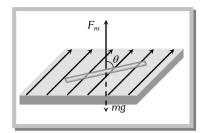
Case 5 : Tension less strings : In the following figure the value and direction of current through the conductor XY so that strings becomes tensionless?

Strings becomes tensionless if weight of conductor XY balanced by magnetic force (F_m) .



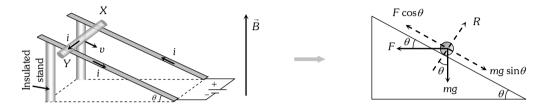
Hence direction of current is from $X \to Y$ and in balanced condition $F_m = mg \implies Bil = mg \implies i = \frac{mg}{Bl}$

Case 6: A current carrying conductor floating in air such that it is making an angle θ with the direction of magnetic field, while magnetic field and conductor both lies in a horizontal plane.



In equilibrium
$$mg = Bil\sin\theta \Rightarrow i = \frac{mg}{Bl\sin\theta}$$

Case 7 : Sliding of conducting rod on inclined rails : When a conducting rod slides on conducting rails.



In the following situation conducting rod (X, Y) slides at constant velocity if

$$F \cos \theta = mg \sin \theta \Rightarrow Bil \cos \theta = mg \sin \theta \Rightarrow B = \frac{mg}{il} \tan \theta$$

• Electric force is an absolute concept while magnetic force is a relative concept for an observer.

• The nature of force between two parallel charge beams decided by electric force, as it is dominator. The nature of force between two parallel charge beams decided by electric force, as it is dominator. The nature of force between two parallel charge beams decided by electric force, as it is dominator. The nature of force between two parallel charge beams decided by electric force, as it is dominator. The nature of force between two parallel charge beams decided by electric force, as it is dominator. The nature of force between two parallel charge beams decided by magnetic force.

is $f_{i_1} = f_{i_2}$

$$f_{i_2} = f_{i_2} = f_{i_1} + f_{i_2} + f_{i_1} + f_{i_2} + f$$

Example

 Example: 46
 A vertical wire carrying a current in the upward direction is placed in a horizontal magnetic field directed towards north. The wire will experience a force directed towards

 (a) North
 (b) South
 (c) East
 (d) West

 Solution : (d)
 By applying Flemings left hand rule, direction of force is found towards west.

 $F \leftarrow i \int ABH$ BH

 $W = S, F \leftarrow E$

- Example: 47 3 A of current is flowing in a linear conductor having a length of 40 cm. The conductor is placed in a magnetic field of strength 500 gauss and makes an angle of 30° with the direction of the field. It experiences a force of magnitude [MP PET 1993]
 - (a) $3 \times 10^4 N$ (b) $3 \times 10^2 N$ (c) $3 \times 10^{-2} N$ (d) $3 \times 10^{-4} N$

Solution : (c) By using $F = Bil \sin \theta \Rightarrow F = (500 \times 10^{-4}) \times 0.4 \times \sin 30^{\circ} \Rightarrow 3 \times 10^{-2} N.$

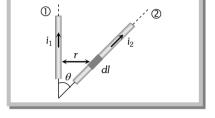
Example: 48 Wires 1 and 2 carrying currents t_1 and t_2 respectively are inclined at an angle θ to each other. What is the force on a small element dl of wire 2 at a distance of r from 1 (as shown in figure) due to the magnetic field of wire 1 [AIEEE 2002]

(a)
$$\frac{\mu_0}{2\pi r} i_1, i_2 dl \tan \theta$$

(b) $\frac{\mu_0}{2\pi r} i_1, i_2 dl \sin \theta$

(c)
$$\frac{\mu_0}{2\pi r}i_1, i_2 dl\cos\theta$$

(d)
$$\frac{\mu_0}{4\pi r} i_1, i_2 \, dl \sin \theta$$

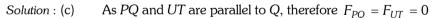


Solution : (c) Length of the component dl which is parallel to wire (1) is $dl \cos \theta$, so force on it

$$F = \frac{\mu_0}{4\pi} \cdot \frac{2i_1i_2}{r} (dl\cos\theta) = \frac{\mu_0i_1i_2dl\cos\theta}{2\pi r}$$

Example: 49 A conductor *PQRSTU*, each side of length *L*, bent as shown in the figure, carries a current *i* and is placed in a uniform magnetic induction *B* directed parallel to the positive Y-axis. The force experience by the wire and its direction are

- (a) 2iBL directed along the negative Z-axis
- (b) 5*iBL* directed along the positive *Z*-axis
- (c) *iBL* direction along the positive Z-axis
- (d) 2iBL directed along the positive Z-axis



The current in TS and RQ are in mutually opposite direction. Hence, $F_{TS} - F_{RQ} = 0$

Therefore the force will act only on the segment SR whose value is Bil and it's direction is +z.

Alternate method :

The given shape of the wire can be replaced by a straight wire of length l between P and U as shown below

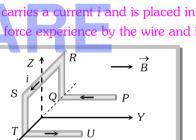
Hence force on replaced wire PU will be F = Bil

and according to FLHR it is directed towards +z-axis



17

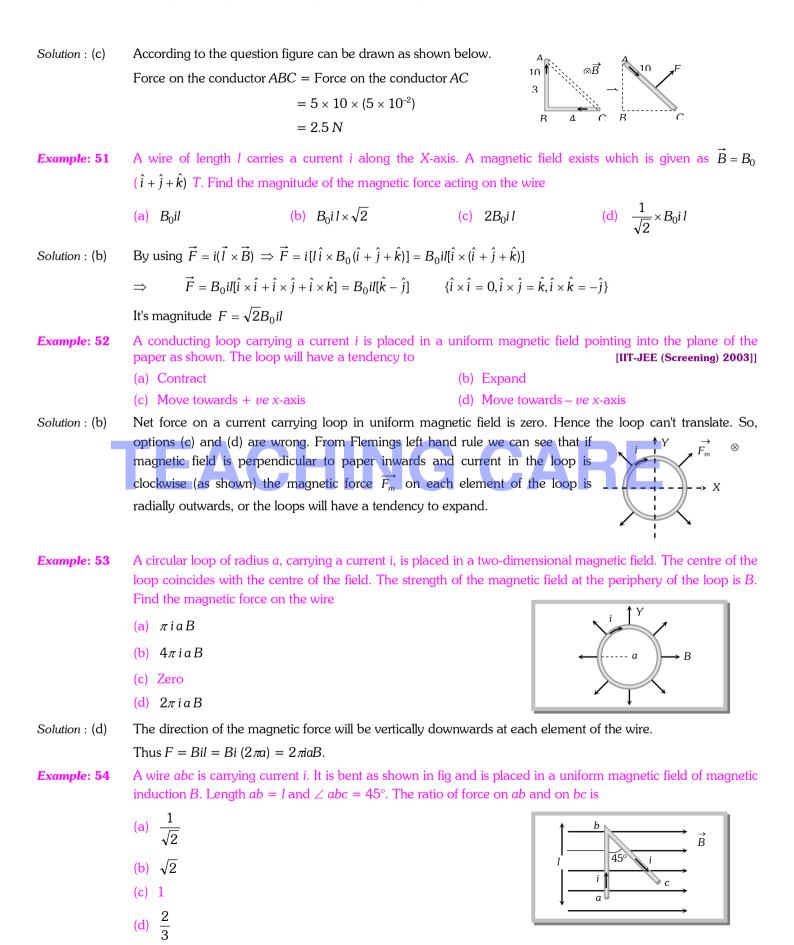
(a) 1.5 N (b) 2.0 N



F P

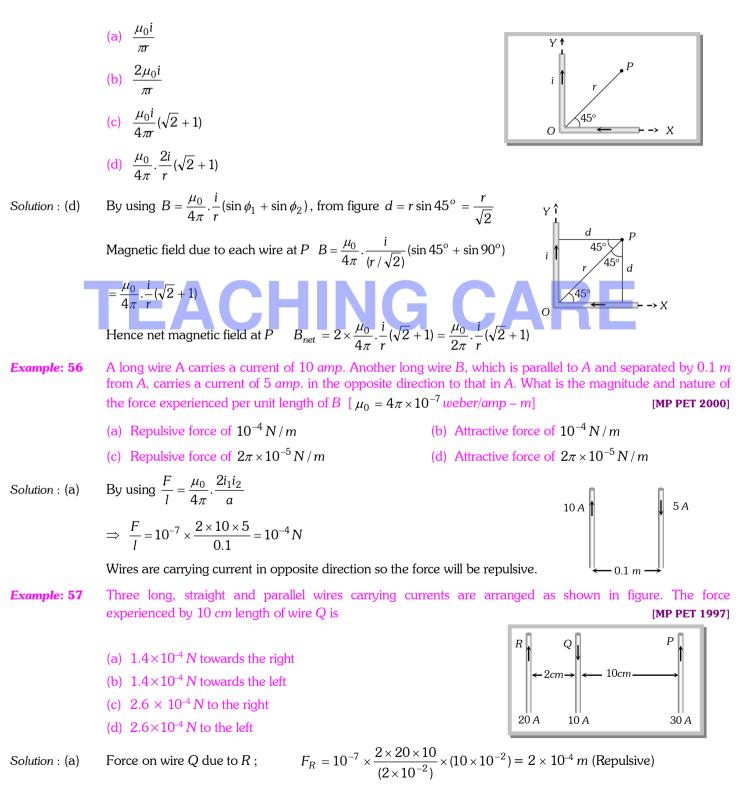
(d) 3.5 N

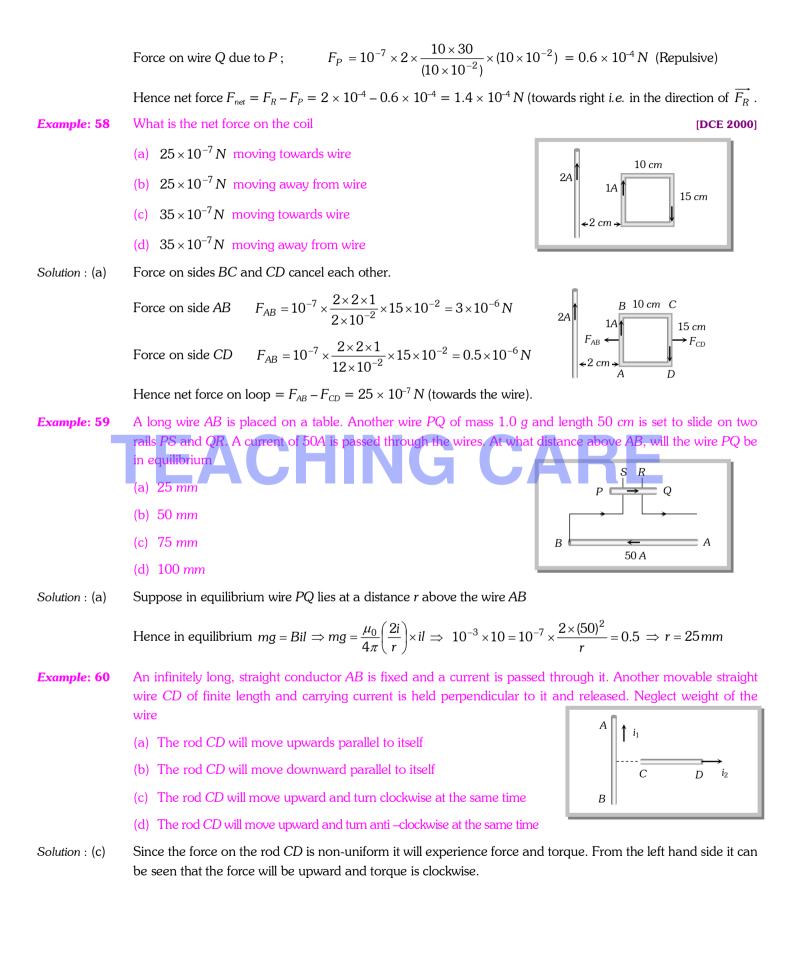
(c) 2.5 N

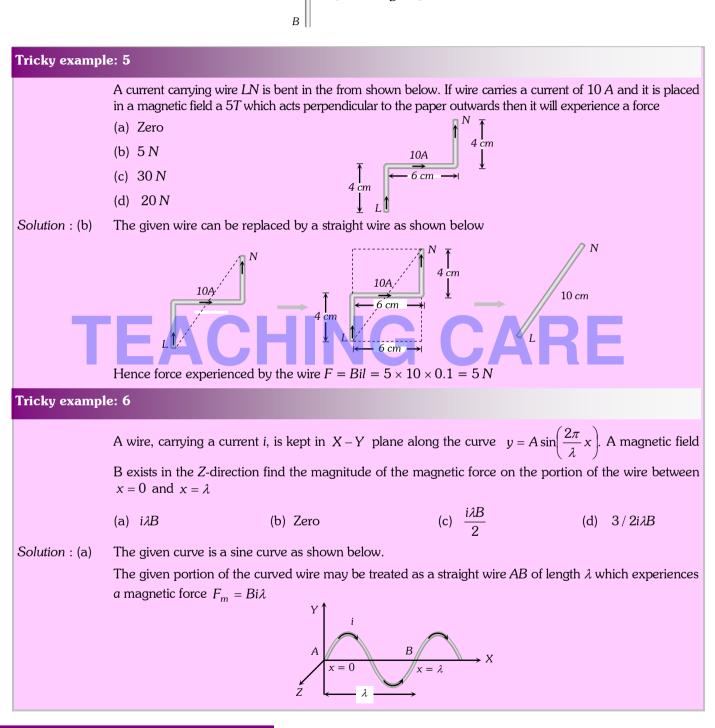


Solution : (c) Force on portion *ab* of wire $F_1 = Bil \sin 90^\circ = Bil$ Force on portion *bc* of wire $F_2 = Bi \left(\frac{l}{\sqrt{2}}\right) \sin 45^\circ = Bil$. So $\frac{F_1}{F_2} = 1$.

Example: 55 Current *i* flows through a long conducting wire bent at right angle as shown in figure. The magnetic field at a point P on the right bisector of the angle XOY at a distance r from O is



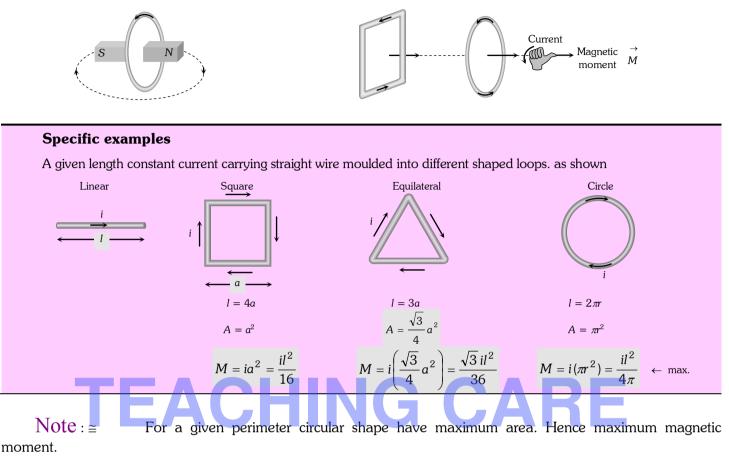




Current Loop As a Magnetic Dipole.

A current carrying circular coil behaves as a bar magnet whose magnetic moment is M = NiA; Where N = Number of turns in the coil, i = Current through the coil and A = Area of the coil

Magnetic moment of a current carrying coil is a vector and it's direction is given by right hand thumb rule



 \cong For a any loop or coil \vec{B} and \vec{M} are always parallel.



Behaviour of Current loop In a Magnetic Field.

(1) Torque

Consider a rectangular current carrying coil *PQRS* having *N* turns and area *A*, placed in a uniform field *B*, in such a way that the normal (\hat{n}) to the coil makes an angle θ with the direction of *B*. the coil experiences a torque given by $\tau = NBiA \sin\theta$. Vectorially $\vec{\tau} = \vec{M} \times \vec{B}$

- (i) τ is zero when $\theta = 0$, *i.e.*, when the plane of the coil is perpendicular to the field.
- (ii) τ is maximum when $\theta = 90^{\circ}$, *i.e.*, the plane of the coil is parallel to the field.

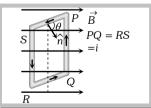
$$\Rightarrow \tau_{\rm max} = NBiA$$

The above expression is valid for coils of all shapes.

(2) Workdone

If coil is rotated through an angle θ from it's equilibrium position then required work. $W = MB(1 - \cos \theta)$. It is maximum when $\theta = 180^{\circ} \Rightarrow W_{\text{max}} = 2 MB$

(3) Potential energy



Is given by $U = -MB \cos\theta \Rightarrow U = \vec{M}.\vec{B}$

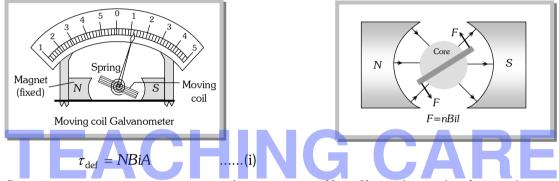
Note : \cong Direction of \vec{M} is found by using Right hand thumb rule according to which curl the fingers of right

hand in the direction of circulation of conventional current, then the thumb gives the direction of \vec{M} .

 \cong Instruments such as electric motor, moving coil galvanometer and tangent galvanometers *etc.* are based on the fact that a current-carrying coil in a uniform magnetic field experiences a torque (or couple).

Moving coil galvanometer.

In a moving coil galvanometer the coil is suspended between the pole pieces of a strong horse-shoe magnet. The pole pieces are made cylinderical and a soft iron cylinderical core is placed within the coil without touching it. This makes the field radial. In such a field the plane of the coil always remains parallel to the field. Therefore $\theta = 90^{\circ}$ and the deflecting torque always has the maximum value.



coil deflects, a restoring torque is set up in the suspension fibre. If α is the angle of twist, the restoring torque is $\tau_{\text{rest}} = C\alpha$ (ii) where *C* is the torsional constant of the fibre.

When the coil is in equilibrium.

$$NBiA = C\alpha \Rightarrow i = \frac{C}{NBA}\alpha \Rightarrow i = K\alpha,$$

Where $K = \frac{C}{NBA}$ is the galvanometer constant. This linear relationship between *i* and α makes the moving coil galvanometer useful for current measurement and detection.

Current sensitivity : The current sensitivity of a galvanometer is defined as the deflection produced in the

$$S_i = \frac{\alpha}{i} = \frac{NBA}{C}$$

galvanometer per unit current flowing through it.

Thus in order to increase the sensitivity of a moving coil galvanometer, N, B and A should be increased and C should be decreased.

Quartz fibres can also be used for suspension of the coil because they have large tensile strength and very low value of k.

Voltage sensitivity (S_v) : Voltage sensitivity of a galvanometer is defined as the deflection produced in the galvanometer per unit applied to it.

$$S_V = \frac{\alpha}{V} = \frac{\alpha}{iR} = \frac{S_i}{R} = \frac{NBA}{RC}$$

	Concepts
-	d in a moving coil galvanometer radial in nature in order to have a linear relation between the current and the deflection.
	ngular current loop is in an arbitrary orientation in an external magnetic field. No work required to rotate the loop about an axis endicular to it's plane.
Moving	coil galvanometer can be made ballistic by using a non-conducting frame (made of ivory or bamboo) instead of a metallic frame.
Example	
Example: 61	A circular coil of radius 4 cm and 20 turns carries a current of 3 ampere. It is placed in a magnetic field of 0.5
	T. The magnetic dipole moment of the coil is [MP PMT 2001] (a) $0.60 A - m^2$ (b) $0.45 A - m^2$ (c) $0.3 A - m^2$ (d) $0.15 A - m^2$
Solution : (c)	$M = niA \Rightarrow M = 20 \times 3 \times \pi (4 \times 10^{-2})^2 = 0.3 A \cdot m^2.$
Example: 62	A steady current <i>i</i> flows in a small square loop of wire of side <i>L</i> in a horizontal plane. The loop is now folded $$
	about its middle such that half of it lies in a vertical plane. Let $\overline{\mu_1}$ and $\overline{\mu_2}$ respectively denote the magnetic
	moments due to the current loop before and after folding. Then [IIT-JEE 1993]
	(a) $\overline{\mu_2} = 0$ (b) $\overline{\mu_1}$ and $\overline{\mu_2}$ are in the same direction
	(c) $\frac{ \overrightarrow{\mu_1} }{ \overrightarrow{\mu_2} } = \sqrt{2}$ (d) $\frac{ \overrightarrow{\mu_1} }{ \overrightarrow{\mu_2} } = \left(\frac{1}{\sqrt{2}}\right)$
Solution : (c)	Initially i CH L_{2} $\downarrow_{\mu_{1} = iL^{2}}$ Finally $\downarrow_{L/2}$
	M = magnetic moment due to each part = $i\left(\frac{L}{2}\right) \times L = \frac{iL^2}{2} = \frac{\mu_1}{2}$
	$\therefore \ \mu_2 = M\sqrt{2} = \frac{\mu_1}{2} \times \sqrt{2} = \frac{\mu_1}{\sqrt{2}}$
Example: 63	A coil of 50 turns is situated in a magnetic field $b = 0.25 weber/m^2$ as shown in figure. A current of 2A is flowing in the coil. Torque acting on the coil will be
	(a) $0.15 N$
	(b) $0.3 N$ $N \stackrel{T}{\checkmark} \stackrel{T}{\cong} \stackrel{T}{\uparrow} S$
	(c) $0.45 N$
	(d) 0.6 N
Solution : (b)	Since plane of the coil is parallel to magnetic field. So $\theta = 90^{\circ}$

Solution : (b)Since plane of the coil is parallel to magnetic field. So $\theta = 90^{\circ}$
Hence $\tau = NBiA \sin 90^{\circ} = NBiA = 50 \times 0.25 \times 2 \times (12 \times 10^{-2} \times 10 \times 10^{-2}) = 0.3 N.$ Example: 64A circular loop of area $1 \ cm^2$, carrying a current of $10 \ A$, is placed in a magnetic field of $0.1 \ T$ perpendicular to
the plane of the loop. The torque on the loop due to the magnetic field is
(a) Zero(b) $10^{-4} N \ m$ (c) $10^{-2} N \ m$ (d) $1 \ N \ m$ Solution : (a) $\tau = NBiA \sin \theta$; given $\theta = 0$ so $\tau = 0$.A circular coil of radius $4 \ cm$ has 50 turns. In this coil a current of $2 \ A$ is flowing. It is placed in a magnetic field
of $0.1 \ weber/m^2$. The amount of work done in rotating it through 180° from its equilibrium position will be

	[CPMT 1977]
Solution : (a)	(a) $0.1 J$ (b) $0.2 J$ (c) 0.4 (d) $0.8 J$ Work done in rotating a coil through an angle θ from it's equilibrium position is $W = MB(1 - \cos\theta)$ where $\theta = 180^{\circ}$
Example: 66	and $M = 50 \times 2 \times \pi (4 \times 10^{-2}) = 50.24 \times 10^{-2} \text{ A-m}^2$. Hence $W = 0.1 J$ A wire of length <i>L</i> is bent in the form of a circular coil and current <i>i</i> is passed through it. If this coil is placed in a magnetic field then the torque acting on the coil will be maximum when the number of turns is (a) As large as possible (b) Any number (c) 2 (d) 1
Solution : (d)	$\tau_{\max} = MB$ or $\tau_{\max} = ni\pi a^2 B$. Let number of turns in length <i>l</i> is <i>n</i> so $l = n(2\pi a)$ or $a = \frac{l}{2\pi n}$
	$\Rightarrow \tau_{\max} = \frac{ni\pi Bl^2}{4\pi^2 n^2} = \frac{l^2 i B}{4\pi n_{\min}} \Rightarrow \tau_{\max} \propto \frac{1}{n_{\min}} \Rightarrow n_{\min} = 1$
Example: 67	A square coil of <i>N</i> turns (with length of each side equal <i>L</i>) carrying current <i>i</i> is placed in a uniform magnetic field $\vec{B} = B_0 \hat{j}$ as shown in figure. What is the torque acting on the coil
	(a) $+B_0NiL^2\hat{k}$ $\vec{B} = B_0\hat{j}$
	(b) $-B_0 NiL^2 \hat{k}$ \uparrow \hat{k}
	(c) $+ B_0 NiL^2 \hat{j}$ (d) $- B_0 NiL^2 \hat{j}$
Solution : (b)	The magnetic field is $\vec{B} = B_0 \hat{j}$ and the magnetic moment $\vec{m} = i\vec{A} = -i(NL^2\hat{i})$
•	The torque is given by $\vec{\tau} = \vec{m} \times \vec{B}$ = $-iNL^2\hat{i} \times B_0\hat{j} = -iNB_0L^2\hat{i} \times \hat{j}$
	$= -iNB_0 L^2 \hat{k}$
Example: 68	The coil of a galvanometer consists of 100 turns and effective area of 1 square cm. The restoring couple is 10^{-8} N-m rad. The magnetic field between the pole pieces is 5 T. The current sensitivity of this galvanometer will be
	[MP PMT 1997] (a) $5 \times 10^4 \text{ rad}/\mu \text{ amp}$ (b) $5 \times 10^{-6} \text{ per amp}$ (c) $2 \times 10^{-7} \text{ per amp}$ (d) $5 \text{ rad}./\mu \text{ amp}$
Solution : (d)	Current sensitivity $(S_i) = \frac{\theta}{i} = \frac{NBA}{C} \Rightarrow \frac{\theta}{i} = \frac{100 \times 5 \times 10^{-4}}{10^{-8}} = 5 \text{ rad } / \mu \text{ amp }.$
Example: 69	The sensitivity of a moving coil galvanometer can be increased by [SCRA 2000]]
	(a) Increasing the number of turns in the coil(b) Decreasing the area of the coil(c) Increasing the current in the coil(d) Introducing a soft iron core inside the coil
Solution : (a)	Sensitivity $(S_i) = \frac{NBA}{C} \Rightarrow S_i \propto N$.

The square loop *ABCD*, carrying a current *i*, is placed in uniform magnetic field *B*, as shown. The loop can rotate about the axis *XX*'. The plane of the loop makes and angle θ ($\theta < 90^{\circ}$) with the direction of *B*. Through what angle will the loop rotate by itself before the torque on it becomes zero (a) θ (b) $90^{\circ}-\theta$ (c) $90^{\circ}+\theta$ (d) $180^{\circ}-\theta$

Tricky example: 7

Solution : (c) In the position shown, *AB* is outside and *CD* is inside the plane of the paper. The Ampere force on *AB* acts into the paper. The torque on the loop will be clockwise, as seen from above. The loop must rotate through an angle $(90^{\circ} + \theta)$ before the plane of the loop becomes normal to the direction of *B* and the torque becomes zero.

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