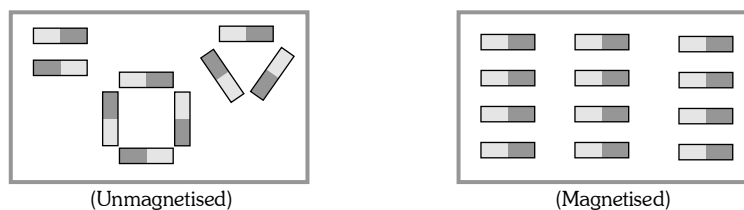


## Magnetism and Matter

The molecular theory of magnetism was given by Weber and modified later by Ewing. According to this theory. Every molecule of a substance is a complete magnet in itself. However, in an **magnetised** substance the molecular magnets are randomly oriented to give zero net magnetic moment. On magnetising, the molecular magnets are realigned in a specific direction leading to a net magnetic moment.



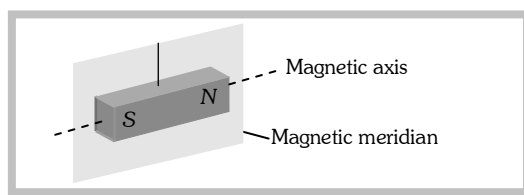
**Note** :  $\cong$  On heating/hammering the magnetism of magnetic substance reduces.

### Bar Magnet.

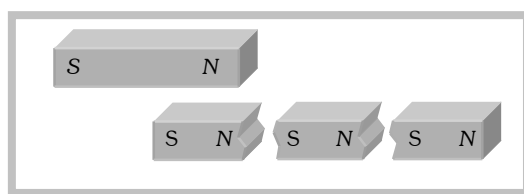
A bar magnet consist of two equal and opposite magnetic pole separated by a small distance. Poles are not exactly at the ends. The shortest distance between two poles is called effective length ( $L_e$ ) and is less then its geometric length ( $L_g$ ).



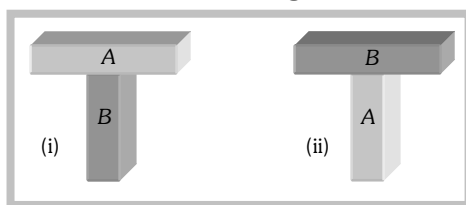
(1) **Directive properties** : When a magnet suspended freely it stays in the earth's N-S direction (in magnetic meridian).



(2) **Monopole concept** : If a magnet is Broken into number of pieces, each piece becomes a magnet. This in turn implies that monopoles do not exist. (i.e., ultimate individual unit of magnetism in any magnet is called dipole).



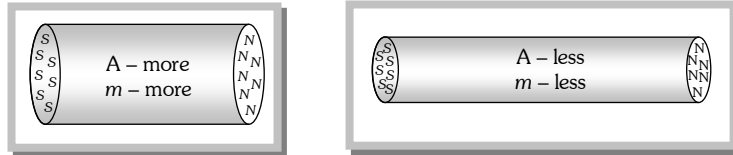
(3) For two rods as shown, if both the rods attract in case (i) and doesn't attract in case (ii) then, B is a magnetic and A is simple iron rod. Repulsion is sure test of magnetism.



## Magnetism and Matter

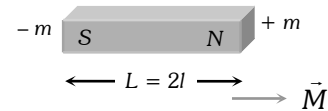
**(4) Pole strength ( $m$ )** : The strength of a magnetic pole to attract magnetic materials towards itself is known as pole strength.

- (i) It is a scalar quantity.
- (ii) Pole strength of  $N$  and  $S$  pole of a magnet is conventionally represented by  $+m$  and  $-m$  respectively.
- (iii) It's SI unit is  $amp \times m$  or  $N/Tesla$  and dimensions are  $[LA]$ .
- (iv) Pole strength of the magnet depends on the nature of material of magnet and area of cross section. It doesn't depend upon length.



**(5) Magnetic moment or magnetic dipole moment ( $\vec{M}$ )** : It represents the strength of magnet. Mathematically it is defined as the product of the strength of either pole and effective length. i.e.  $\vec{M} = m(2\vec{l})$

- (i) It is a vector quantity directed from south to north.
- (ii) It's S.I. unit  $amp \times m^2$  or  $N-m/Tesla$  and dimensions  $[AL^2]$
- (iii) Magnetic moment in various other situations.



**Current carrying coil**

Magnetic moment  $M = NiA$   
 $N$  = number of turns,  
 $i$  = current through the coil,  $A$  = Area of the coil

**Combination of bar magnet**

$$M_{net} = \sqrt{M_1^2 + M_2^2 + 2M_1M_2 \cos \theta}$$

$$\tan \alpha = \frac{M_2 \sin \theta}{M_1 + M_2 \cos \theta}$$

**Revolving charge**

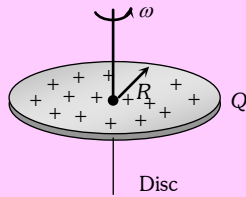
(a) Orbital electron : In an atom electrons revolve around the nucleus in circular orbit and it is equivalent to the flow of current in the orbit. Thus the orbit of electrons is considered as tiny current loop with magnetic moment.

$$M = eivA = \frac{e\omega r^2}{2} = \frac{1}{2}evr = \frac{e}{2m}L = \frac{eh}{4\pi m}$$

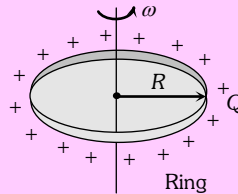
where,  $\omega$  = angular speed,  $\nu$  = frequency,  $v$  = linear speed and  $L$  = Angular momentum  $I\omega$ .

## Magnetism and Matter

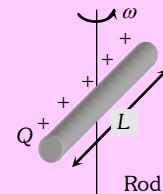
(b) For geometrical symmetrical charged rotating bodies : The magnetic moment given by  $M = \frac{QL}{2m} = \frac{QI\omega}{2m}$ ; where  $m$  = mass of rotating body,  $Q$  = charge on body,  $I$  = moment of inertia of rotating body about axis of rotation.



$$I = \frac{mR^2}{2}, \quad M = \frac{1}{4} Q\omega R^2$$



$$I = MR^2, \quad M = \frac{1}{2} Q\omega R^2$$



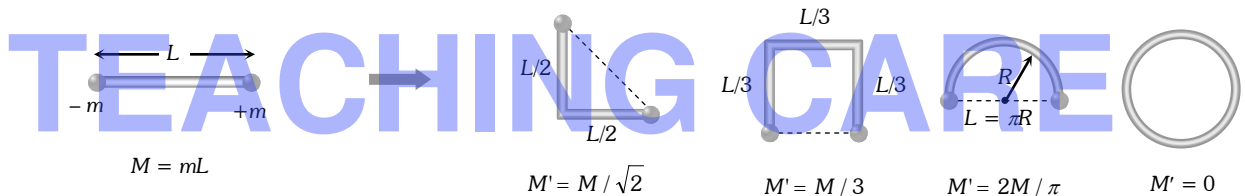
$$I = \frac{mL^2}{12}, \quad M = \frac{1}{24} Q\omega L^2$$

**Note :**  $\cong$  Bohr magneton  $\mu_B = \frac{eh}{4\pi m} = 9.27 \times 10^{-24} \text{ A/m}^2$ . It serves as natural unit of magnetic moment. Bohr magneton can be defined as the orbital magnetic moment of an electron circulating in inner most orbit.

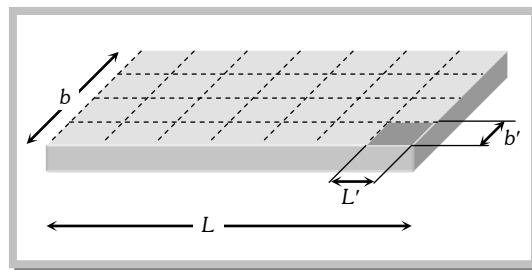
$\cong$  Magnetic moment of straight current carrying wire is zero.

$\cong$  Magnetic moment of toroid is zero.

$\cong$  If a magnetic wire of magnetic moment ( $M$ ) is bent into any shape then it's  $M$  decreases as it's length ( $L$ ) always decreases and pole strength remains constant.



**(6) Cutting of a bar magnet :** Suppose we have a rectangular bar magnet having length, breadth and mass are  $L$ ,  $b$  and  $w$  respectively if it is cut in  $n$  equal parts along the length as well as perpendicular to the length simultaneously as shown in the figure then



Length of each part  $L' = \frac{L}{\sqrt{n}}$ , breadth of each part  $b' = \frac{b}{\sqrt{n}}$ , Mass of each part  $w' = \frac{w}{n}$ , pole strength of each

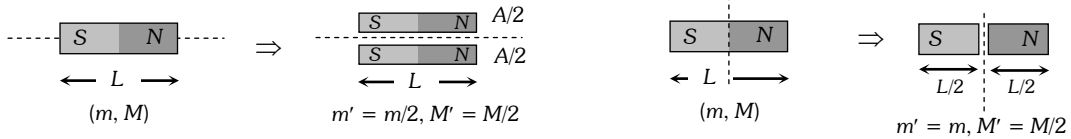
part  $m' = \frac{m}{\sqrt{n}}$ , Magnetic moment of each part  $M' = m' L' = \frac{m}{\sqrt{n}} \times \frac{L}{\sqrt{n}} = \frac{M}{n}$

If initially moment of inertia of bar magnet about the axes passing from centre and perpendicular to it's length is  $I = w \left( \frac{L^2 + b^2}{12} \right)$  then moment of inertia of each part  $I' = \frac{I}{n^2}$

**Note :**  $\cong$  For short bar magnet  $b = 0$  so  $L' = \frac{L}{n}$ ,  $w' = \frac{w}{n}$ ,  $m' = m$ ,  $M' = \frac{M}{n}$  and  $I' = \frac{I}{n^3}$

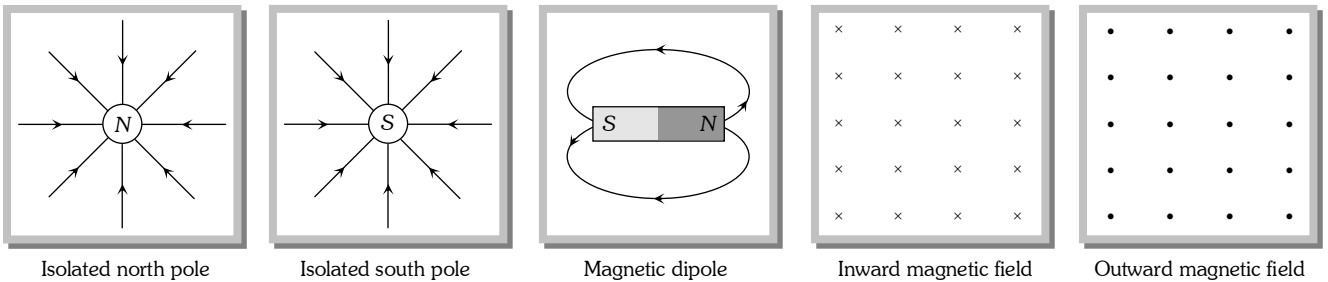
## Magnetism and Matter

≅ Commonly asked question



### Various Terms Related to Magnetism.

**(1) Magnetic field and magnetic lines of force** : Space around a magnetic pole or magnet or current carrying wire within which its effect can be experienced is defined magnetic field. Magnetic field can be represented with the help of a set of lines or curves called magnetic lines of force.



### (2) Magnetic flux ( $\phi$ ) and flux density ( $B$ )

(i) The number of magnetic lines of force passing normally through a surface is defined as magnetic flux ( $\phi$ ). Its S.I. unit is *weber (wb)* and CGS unit is *Maxwell*.

Remember  $1 \text{ wb} = 10^8 \text{ maxwell}$ .

(ii) When a piece of a magnetic substance is placed in an external magnetic field the substance becomes magnetised. The number of magnetic lines of induction inside a magnetised substance crossing unit area normal to their direction is called magnetic induction or magnetic flux density ( $\vec{B}$ ). It is a vector quantity.

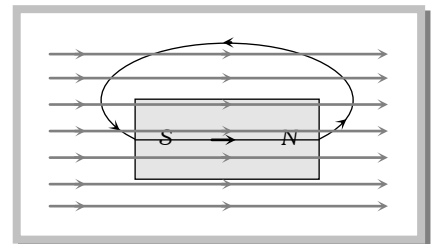
Its SI unit is *Tesla* which is equal to

$$\frac{\text{wb}}{\text{m}^2} = \frac{\text{N}}{\text{amp} \times \text{m}} = \frac{\text{J}}{\text{amp} \times \text{m}^2} = \frac{\text{volt} \times \text{sec}}{\text{m}^2}$$

and CGS unit is *Gauss*. Remember  $1 \text{ Tesla} = 10^4 \text{ Gauss}$ .

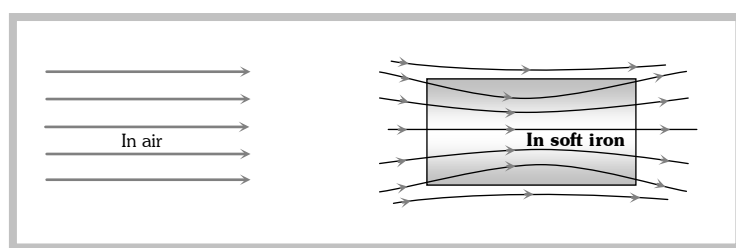
**Note** : ≅ Magnetic flux density can also be defined in terms of force

experienced by a unit north pole placed in that field i.e.  $B = \frac{F}{m_0}$ .



**(3) Magnetic permeability** : It is the degree or extent to which magnetic lines of force can enter a substance and is denoted by  $\mu$ .

Characteristic of a medium which allows magnetic flux to pass through it is called its permeability. e.g. permeability of soft iron is 1000 times greater than that of air.



## Magnetism and Matter

Also  $\mu = \mu_0 \mu_r$ ; where  $\mu_0$  = absolute permeability of air or free space =  $4\pi \times 10^{-7}$  tesla  $\times$  m / amp.

and  $\mu_r$  = Relative permeability of the medium =  $\frac{B}{B_0} = \frac{\text{flux density in material}}{\text{flux density in vacuum}}$ .

**(4) Intensity of magnetising field ( $\vec{H}$ ) (magnetising field)** : It is the degree or extent to which a magnetic field can magnetise a substance. Also  $H = \frac{B}{\mu}$ .

It's SI unit is  $A/m$ . =  $\frac{N}{m^2 \times \text{Tesla}} = \frac{N}{wb} = \frac{J}{m^3 \times \text{Tesla}} = \frac{J}{m \times wb}$  It's CGS unit is Oersted. Also 1oersted = 80 A/m

**(5) Intensity of magnetisation ( $I$ )** : It is the degree to which a substance is magnetised when placed in a magnetic field.

It can also be defined as the pole strength per unit cross sectional area of the substance or the induced dipole moment per unit volume.

Hence  $I = \frac{m}{A} = \frac{M}{V}$ . It is a vector quantity, it's S.I. unit is Amp/m.

**(6) Magnetic susceptibility ( $\chi_m$ )** : It is the property of the substance which shows how easily a substance can be magnetised. It can also be defined as the ratio of intensity of magnetisation ( $I$ ) in a substance to the magnetic intensity ( $H$ ) applied to the substance, i.e.  $\chi_m = \frac{I}{H}$ . It is a scalar quantity with no units and dimensions.

**(7) Relation between permeability and susceptibility** : Total magnetic flux density  $B$  in a material is the sum of magnetic flux density in vacuum  $B_0$  produced by magnetising force and magnetic flux density due to magnetisation of material  $B_m$ . i.e.  $B = B_0 + B_m$

$\Rightarrow B = \mu_0 H + \mu_0 I = \mu_0 (H + I) = \mu_0 H (1 + \chi_m)$ . Also  $\mu_r = (1 + \chi_m)$

**Note** :  $\cong$  In CGS  $B = H + 4\pi I$  and  $\mu = 1 + 4\pi\chi_m$ .

### Force and Field.

**(1) Coulombs law in magnetism** : The force between two magnetic poles of strength  $m_1$  and  $m_2$  lying at a distance  $r$  is given by  $F = k \cdot \frac{m_1 m_2}{r^2}$ . In S.I. units  $k = \frac{\mu_0}{4\pi} = 10^{-7} \text{wb} / \text{Amp} \times \text{m}$ , In CGS units  $k = 1$

#### (2) Magnetic field

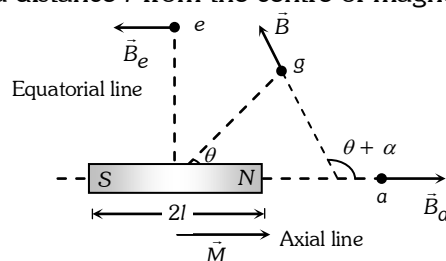
(i) Magnetic field due to an imaginary magnetic pole (Pole strength  $m$ ) : Is given by  $B = \frac{F}{m_0}$  also  $B = \frac{\mu_0}{4\pi} \cdot \frac{m}{d^2}$

(ii) Magnetic field due to a bar magnet : At a distance  $r$  from the centre of magnet

(a) On axial position

$$B_a = \frac{\mu_0}{4\pi} \frac{2Mr}{(r^2 - l^2)^2};$$

$$\text{If } l \ll r \text{ then } B_a = \frac{\mu_0}{4\pi} \frac{2M}{r^3}$$



## Magnetism and Matter

(b) On equatorial position :  $B_e = \frac{\mu_0}{4\pi} \frac{M}{(r^2 + l^2)^{3/2}}$  ; If  $l \ll r$  ; then  $B_e = \frac{\mu_0}{4\pi} \frac{M}{r^3}$

(c) General position : In general position for a short bar magnet  $B_g = \frac{\mu_0}{4\pi} \frac{M}{r^3} \sqrt{(3 \cos^2 \theta + 1)}$

**(3) Bar magnet in magnetic field :** When a bar magnet is left free in an uniform magnetic field, it aligns itself in the direction of the field.

(i) Torque :  $\tau = MB \sin \theta \Rightarrow \vec{\tau} = \vec{M} \times \vec{B}$

(ii) Work :  $W = MB(1 - \cos \theta)$

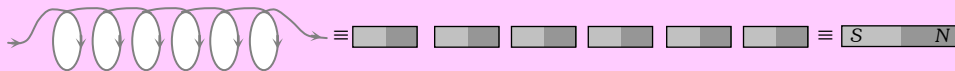
(iii) Potential energy :  $U = MB \cos \theta = -\vec{M} \cdot \vec{B}$  ; ( $\theta$  = Angle made by the dipole with the field)

**Note :** ≡ For more details see comparative study of electric and magnetic dipole in electrostatics.

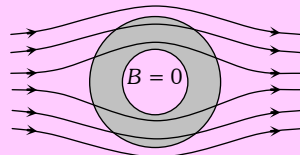
**(4) Gauss's law in magnetism :** Net magnetic flux through any surface is always zero i.e.  $\oint \vec{B} \cdot d\vec{s} = 0$

### Concepts

- The property of magnetism in materials is on account of magnetic moment in the material.
- Atoms which have paired electrons have the magnetic moment zero.
- **Magnetostriction :** The length of an iron bar changes when it is magnetised, when an iron bar is magnetised its length increases due to alignment of spins parallel to the field. This increase is in the direction of magnetisation. This effect is known as magnetostriction.
- A current carrying solenoid can be treated as the arrangement of small magnetic dipoles placed in line with each other as shown. The number of such small magnetic dipoles is equal to the number of turns in the solenoid.



- When a magnetic dipole of moment  $M$  moves from unstable equilibrium to stable equilibrium position in a magnetic field  $B$ , the kinetic energy by it will be  $2 MB$ .
- Intensity of magnetisation ( $I$ ) is produced in materials due to spin motion of electrons.
- For protecting sensitive equipment from the external magnetic field it should be placed inside an iron core. (magnetic shielding)



### Example

**Example: 1** The work done in turning a magnet of magnetic moment  $M$  by an angle of  $90^\circ$  from the meridian, is  $n$  times the corresponding work done to turn it through an angle of  $60^\circ$ . The value of  $n$  is given by [MP PET 2003]

- (a) 2                                      (b) 1                                      (c) 1/2                                      (d) 1/4

**Solution :** (a)  $W = MB(1 - \cos \theta) \Rightarrow W_{0^\circ \rightarrow 90^\circ} = n \times (W_{0^\circ \rightarrow 60^\circ}) \Rightarrow MB(1 - \cos 90^\circ) = n \times MB(1 - \cos 60^\circ) \Rightarrow n = 2$

## Magnetism and Matter

**Example: 2** The magnetic susceptibility of a material of a rod is 499, permeability of vacuum is  $4\pi \times 10^{-7} \text{ H/m}$ . Permeability of the material of the rod in henry/metre is [EAMCET 2003]

- (a)  $\pi \times 10^{-4}$                       (b)  $2\pi \times 10^{-4}$                       (c)  $3\pi \times 10^{-4}$                       (d)  $4\pi \times 10^{-4}$

Solution : (b)  $\mu_r = (1 + \gamma_m) \Rightarrow \mu_r = (1 + 499) = 500$  Also  $\mu = \mu_0 \mu_r = 4\pi \times 10^{-7} \times 500 = 2\pi \times 10^{-4}$

**Example: 3** A magnetic needle lying parallel to a magnetic field requires  $W$  units of work to turn it through  $60^\circ$ . The torque required to maintain the needle in this position will be [MNR 1991; KCET 1994; MP PET 1996; AIEEE 2003]

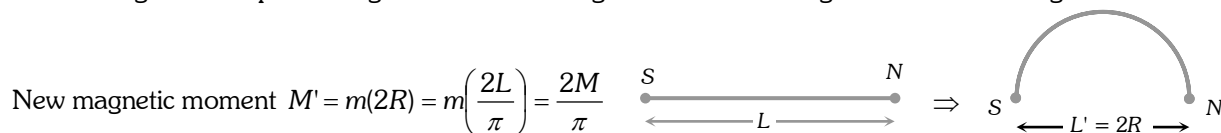
- (a)  $\sqrt{3} W$                       (b)  $-W$                       (c)  $\frac{\sqrt{3}}{2} W$                       (d)  $2W$

Solution : (a)  $\tau = MB \sin \theta$  and  $W = MB(1 - \cos \theta) \Rightarrow W = MB(1 - \cos 60^\circ) = \frac{MB}{2}$ . Hence  $\tau = MB \sin 60^\circ = \frac{\sqrt{3} MB}{2} = \sqrt{3} W$

**Example: 4** An iron rod of length  $L$  and magnetic moment  $M$  is bent in the form of a semicircle. Now its magnetic moment will be [CPMT 1984; MP Board 1986; NCERT 1975; MP PET/PMT 1988; EAMCET (Med.) 1995; Manipal MEE 1995; RPMT 1996; BHU 1995; MP PMT 2002]

- (a)  $M$                       (b)  $\frac{2M}{\pi}$                       (c)  $\frac{M}{\pi}$                       (d)  $M\pi$

Solution : (b) On bending a rod its pole strength remains unchanged where as its magnetic moment changes



**Example: 5** A short bar magnet with its north pole facing north forms a neutral point at  $P$  in the horizontal plane. If the magnet is rotated by  $90^\circ$  in the horizontal plane, the net magnetic induction at  $P$  is : (Horizontal component of earth's magnetic field =  $B_H$ ) [EAMCET (Engg.) 2000]

- (a) 0                      (b)  $2B_H$                       (c)  $\frac{\sqrt{5}}{2} B_H$                       (d)  $\sqrt{5} B_H$

Solution : (d)

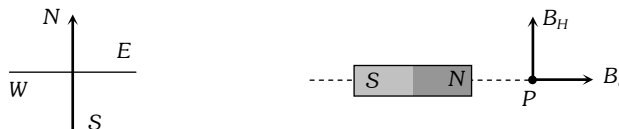
**Initially**



Neutral point is obtained on equatorial line and at neutral point  $|B_H| = |B_e|$

Where  $B_H$  = Horizontal component of earth's magnetic field and  $B_e$  = Magnetic field due to bar magnet on its equatorial line

**Finally**



Point  $P$  comes on axial line of the magnet and at  $P$ , net magnetic field

$$B = \sqrt{B_H^2 + B_a^2} = \sqrt{(2B_e)^2 + (B_H)^2} = \sqrt{(2B_H)^2 + B_H^2} = \sqrt{5} B_H$$

**Example: 6** A bar magnet of magnetic moment  $3.0 \text{ Amp} \times \text{m}$  is placed in a uniform magnetic induction field of  $2 \times 10^{-5} \text{ T}$ . If each pole of the magnet experiences a force of  $6 \times 10^{-4} \text{ N}$  the length of the magnet is [EAMCET (Med.) 2000]

- (a) 0.5 m                      (b) 0.3 m                      (c) 0.2 m                      (d) 0.1 m

Solution : (d)  $M = mL$  and  $F = mB, \Rightarrow F = \frac{M}{L} \times B \Rightarrow 6 \times 10^{-4} = \frac{3}{L} \times 2 \times 10^{-5} \Rightarrow L = 0.1 \text{ m}$

**Example: 7** Force between two identical bar magnets whose centres are  $r$  metre apart is 4.8 N when their axes are in the same line. If the separation is increases to  $2r$  metre, the force between them is reduced to

[AIIMS 1995; Pb. CET 1997]

## Magnetism and Matter

- (a) 2.4 N                      (b) 1.2 N                      (c) 0.6 N                      (d) 0.3 N

**Solution :** (d) Force between two bar magnet  $F \propto \frac{1}{d^4} \Rightarrow \frac{F_1}{F_2} = \left(\frac{d_2}{d_1}\right)^4 \Rightarrow \frac{4.8}{F_2} = \left(\frac{2r}{r}\right)^2 \Rightarrow F_2 = 0.3N$  Where  $d =$  separation between magnets.

**Example: 8** Two identical magnetic dipoles of magnetic moments  $1.0 \text{ A}\cdot\text{m}^2$  each, placed at a separation of  $2\text{m}$  with their axis perpendicular to each other. The resultant magnetic field at a point midway between the dipoles is [Roorkee 1995]

- (a)  $5 \times 10^{-7} \text{ T}$                       (b)  $\sqrt{5} \times 10^{-7} \text{ T}$                       (c)  $\frac{T}{2}$                       (d) None of these

**Solution :** (b)  $B_1 = \frac{\mu_0}{4\pi} \cdot \frac{2M}{\left(\frac{r}{2}\right)^3} = 10^{-7} \times \frac{2 \times 1}{\left(\frac{2}{2}\right)^3}; B_2 = \frac{\mu_0}{4\pi} \cdot \frac{M}{\left(\frac{r}{2}\right)^3} = 10^{-7} \times \frac{1}{\left(\frac{2}{2}\right)^3}; B_{net} = \sqrt{(2 \times 10^{-7})^2 + (10^{-7})^2} = \sqrt{5} \times 10^{-7} \text{ T}$

**Example: 9** A magnet of magnetic moment  $20 \text{ C.G.S. units}$  is freely suspended in a uniform magnetic field of intensity  $0.3 \text{ C.G.S. units}$ . The amount of work done in deflecting it by an angle of  $30^\circ$  in C.G.S. units is [MP PET 1991]

- (a) 6                      (b)  $3\sqrt{3}$                       (c)  $3(2 - \sqrt{3})$                       (d) 3

**Solution :** (c)  $W = MB(1 - \cos\theta) \Rightarrow W = 20 \times 0.3(1 - \cos 30^\circ) = 3(2 - \sqrt{3})$

**Example: 10** The magnetic field at a point X on the axis of a small bar magnet is equal to the field at a point Y on the equator of the same magnet. The ratio of the distance of X and Y from the centre of the magnet is [MP PMT 1990]

- (a)  $2^{-3}$                       (b)  $2^{-1/3}$                       (c)  $2^3$                       (d)  $2^{1/3}$

**Solution :** (d) Suppose distances of points X and Y from magnet are  $x$  and  $y$  respectively then According to question  $B_{axial} = B_{equatorial} \Rightarrow \frac{\mu_0}{4\pi} \cdot \frac{2M}{x^3} = \frac{\mu_0}{4\pi} \cdot \frac{M}{y^3} \Rightarrow \frac{x}{y} = \frac{2^{1/3}}{1}$

**Example: 11** A magnetising field of  $2000 \text{ A/m}$  produces a flux  $6.28 \times 10^{-4} \text{ weber}$  in a rod. If the area of cross-section is  $2 \times 10^{-5} \text{ m}^2$ . Then the relative permeability of the substance is

- (a)  $0.75 \times 10^{-2}$                       (b)  $1.25 \times 10^4$                       (c) 0.25                      (d) 1.01

**Solution :** (b) By using  $B = \mu_0 \mu_r H$  and  $B = \frac{\phi}{A}, \Rightarrow \mu_r = \frac{\phi}{A \mu_0 H} = \frac{6.28 \times 10^{-4}}{2 \times 10^{-5} \times 4\pi \times 10^{-7} \times 2000} = 1.25 \times 10^4$

**Example: 12** Due to a small magnet intensity at a distance  $x$  in the end on position is  $9 \text{ Gauss}$ . What will be the intensity at a distance  $\frac{x}{2}$  on broad side on position

- (a) 9 Gauss                      (b) 4 Gauss                      (c) 36 Gauss                      (d) 4.5 Gauss

**Solution :** (c) In C.G.S.  $B_{axial} = 9 = \frac{2M}{x^3}$  .....(i)  $B_{equatorial} = \frac{M}{\left(\frac{x}{2}\right)^3} = \frac{8M}{x^3}$  .....(ii)

From equation (i) and (ii)  $B_{equatorial} = 36 \text{ Gauss}$ .

**Example: 13** The magnetic moment produced in a substance of  $1\text{gm}$  is  $6 \times 10^{-7} \text{ ampere-metre}^2$ . If its density is  $5 \text{ gm/cm}^3$ , then the intensity of magnetisation in  $\text{A/m}$  will be

- (a)  $8.3 \times 10^6$                       (b) 3.0                      (c)  $1.2 \times 10^{-7}$                       (d)  $3 \times 10^{-6}$

**Solution :** (b)  $I = \frac{M}{V} = \frac{M}{\text{mass/density}}$ , given mass =  $1\text{gm} = 10^{-3}\text{kg}$ , and density =  $5\text{gm/cm}^3 = \frac{5 \times 10^{-3}\text{kg}}{(10^{-2})^3\text{m}^3} = 5 \times 10^3 \text{ kg/m}^3$



## Magnetism and Matter

Hence  $I = \frac{6 \times 10^{-7} \times 5 \times 10^3}{10^{-3}} = 3$

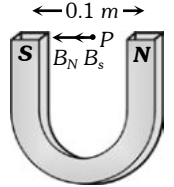
**Example: 14** The distance between the poles of a horse shoe magnet is 0.1 m and its pole strength is 0.01 amp-m. The induction of magnetic field at a point midway between the poles will be

- (a)  $2 \times 10^{-5} T$                       (b)  $4 \times 10^{-6} T$                       (c)  $8 \times 10^{-7} T$                       (d) Zero

**Solution :** (c) Net magnetic field at mid point P,  $B = B_N + B_S$

where  $B_N$  = magnetic field due to N- pole       $B_S$  = magnetic field due to S- pole

$$B_N = B_S = \frac{\mu_0}{4\pi} \frac{m}{r^2} = 10^{-7} \times \frac{0.01}{\left(\frac{0.1}{2}\right)^2} = 4 \times 10^{-7} T \quad \therefore B_{net} = 8 \times 10^{-7} T.$$



**Example: 15** A cylindrical rod magnet has a length of 5 cm and a diameter of 1 cm. It has a uniform magnetisation of  $5.30 \times 10^3 \text{ Amp/m}$ . What its magnetic dipole moment

- (a)  $1 \times 10^{-2} J/T$                       (b)  $2.08 \times 10^{-2} J/T$                       (c)  $3.08 \times 10^{-2} J/T$                       (d)  $1.52 \times 10^{-2} J/T$

**Solution :** (b) Relation for dipole moment is,  $M = I \times V$ , Volume of the cylinder  $V = \pi r^2 l$ , Where  $r$  is the radius and  $l$  is the length of the cylinder, then dipole moment,

$$M = I \times \pi r^2 l = (5.30 \times 10^3) \times \frac{22}{7} \times (0.5 \times 10^{-2})^2 (5 \times 10^{-2}) = 2.08 \times 10^{-2} J/T$$

**Example: 16** A bar magnet has a magnetic moment of  $2.5 J T^{-1}$  and is placed in a magnetic field of  $0.2 T$ . Work done in turning the magnet from parallel to anti-parallel position relative to field direction is

- (a) 0.5J                                      (b) 1J    (c) 2J    (d) 0J

**Solution :** (b) Work done,  $W = -MB(\cos \theta_2 - \cos \theta_1) = -MB(\cos 180^\circ - \cos 0^\circ) = -MB(-1 - 1) = 2MB = 2 \times 2.5 \times 0.2 = 1J$

**Example: 17** A bar magnet with its poles 25 cm apart and of pole strength 24 amp-m rests with its centre on a frictionless pivot. A force  $F$  is applied on the magnet at a distance of 12 cm from the pivot so that it is held in equilibrium at an angle of  $30^\circ$  with respect to a magnetic field of induction 0.25 T. The value of force  $F$  is

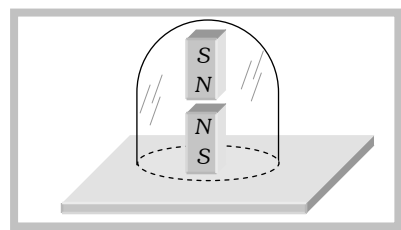
- (a) 5.62 N                                      (b) 2.56 N                                      (c) 6.52 N                                      (d) 6.25 N

**Solution :** (d) In equilibrium

$$\text{Magnetic torque} = \text{Deflecting torque} \Rightarrow MB \sin \theta = F.d \text{ or } F = \frac{mB \sin \theta}{d} = \frac{24 \times 0.25 \times 0.25 \sin 30^\circ}{0.12} = 6.25 N$$

**Example: 18** Two identical bar magnets with a length 10 cm and weight 50 gm – weight are arranged freely with their like poles facing in a arranged vertical glass tube. The upper magnet hangs in the air above the lower one so that the distance between the nearest pole of the magnet is 3mm. Pole strength of the poles of each magnet will be

- (a) 6.64 amp × m  
 (b) 2 amp × m  
 (c) 10.25 amp × m  
 (d) None of these



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Solution : (a) The weight of upper magnet should be balanced by the repulsion between the two magnet

$$\therefore \frac{\mu}{4\pi} \cdot \frac{m^2}{r^2} = 50gm - wt \Rightarrow 10^{-7} \times \frac{m^2}{(9 \times 10^{-6})} = 50 \times 10^{-3} \times 9.8 \Rightarrow m = 6.64 \text{ amp} \times m$$

### Tricky Example: 1

A bar magnet of magnetic moment  $2.0 \text{ A}\cdot\text{m}^2$  is free to rotate about a vertical axis passing through its centre. The magnet is released from rest from east-west position. Then the kinetic energy of the magnet as it takes north-south position is (Horizontal component of earth's field is  $25 \mu \text{ T}$ )

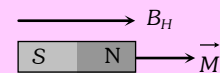
[EAMCET (Engg.) 1996]

- (a)  $25 \mu \text{ J}$                       (b)  $50 \mu \text{ J}$                       (c)  $100 \mu \text{ J}$                       (d)  $12.5 \mu \text{ J}$

Solution : (b) When a bar magnet suspended freely in earth's magnetic field, it always align itself in the direction of field (i.e. along N - S direction)

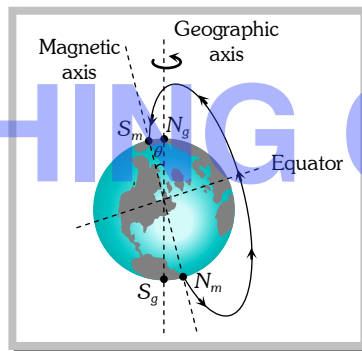
So by using  $U = -MB_H \cos \theta$ ; where  $\theta =$  angle between  $M$  and  $B_H$

$$U = -M \times B \cos 0 = -2 \times 25 = -50 \mu \text{ J}$$



### Earth's magnetic Field (Terrestrial Magnetism).

As per the most established theory it is due to the rotation of the earth where by the various charged ions present in the molten state in the core of the earth rotate and constitute a current.



(1) The magnetic field of earth is similar to one which would be obtained if a huge magnet is assumed to be buried deep inside the earth at its centre.

(2) The axis of rotation of earth is called geographic axis and the points where it cuts the surface of earth are called geographical poles ( $N_g, S_g$ ). The circle on the earth's surface perpendicular to the geographical axis is called equator.

(3) A vertical plane passing through the geographical axis is called geographical meridian.

(4) The axis of the huge magnet assumed to be lying inside the earth is called magnetic axis of the earth. The points where the magnetic axis cuts the surface of earth are called magnetic poles. The circle on the earth's surface perpendicular to the magnetic axis is called magnetic equator.

(5) Magnetic axis and Geographical axis don't coincide but they make an angle of  $17.5^\circ$  with each other.

(6) Magnetic equator divides the earth into two hemispheres. The hemisphere containing south polarity of earth's magnetism is called northern hemisphere while the other, the southern hemisphere.

(7) The magnetic field of earth is not constant and changes irregularly from place to place on the surface of the earth and even at a given place it varies with time too.

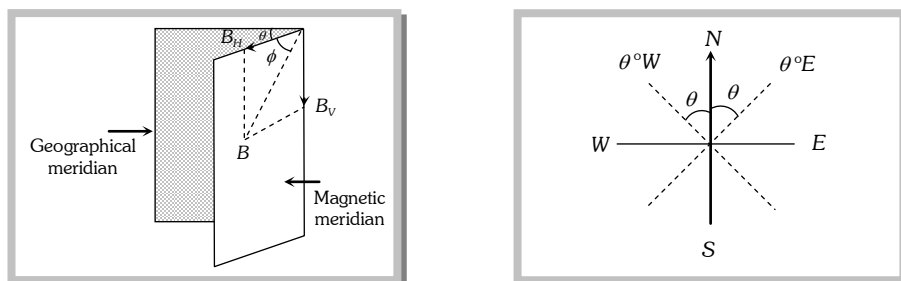
(8) Direction of earth's magnetic field is from S (geographical south) to N (Geographical north).

## Magnetism and Matter

### Elements of Earth's Magnetic Field.

The magnitude and direction of the magnetic field of the earth at a place are completely given by certain quantities known as magnetic elements.

(1) **Magnetic Declination ( $\theta$ )** : It is the angle between geographic and the magnetic meridian planes.



Declination at a place is expressed at  $\theta^\circ E$  or  $\theta^\circ W$  depending upon whether the north pole of the compass needle lies to the east or to the west of the geographical axis.

(2) **Angle of inclination or Dip ( $\phi$ )** : It is the angle between the direction of intensity of total magnetic field of earth and a horizontal line in the magnetic meridian.

(3) **Horizontal component of earth's magnetic field ( $B_H$ )** : Earth's magnetic field is horizontal only at the magnetic equator. At any other place, the total intensity can be resolved into horizontal component ( $B_H$ ) and vertical component ( $B_V$ ).

$$\text{Also } B_H = B \cos \phi \dots\dots (i) \quad \text{and} \quad B_V = B \sin \phi \dots\dots (ii)$$

$$\text{By squaring and adding equation (i) and (ii) } B = \sqrt{B_H^2 + B_V^2}$$

$$\text{Dividing equation (ii) by equation (i) } \tan \phi = \frac{B_V}{B_H}$$

**Note** :  $\cong$  At equator  $\theta = 0 \Rightarrow B_H = B, B_V = 0$  while at poles  $\phi = 90^\circ \Rightarrow B_H = 0, B_V = B$ .

### Magnetic Maps and Neutral Points.

(1) Magnetic maps (*i.e.* Declination, dip and horizontal component) over the earth vary in magnitude from place to place. It is found that many places have the same value of magnetic elements. The lines are drawn joining all place on the earth having same value of a magnetic elements. These lines forms magnetic map.

(i) Isogonic lines: These are the lines on the magnetic map joining the places of equal declination.

(ii) Agonic line: The line which passes through places having zero declination is called agonic line.

(iii) Isoclinic lines : These are the lines joining the points of equal dip or inclination.

(iv) Aclinic line : The line joining places of zero dip is called aclinic line (or magnetic equator)

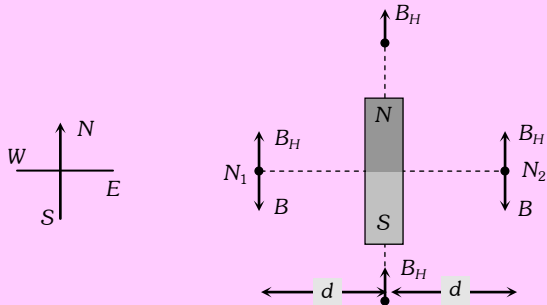
(v) Isodynamic lines : The lines joining the points or places having the same value of horizontal component of earth's magnetic field are called isodynamic lines.

(2) **Neutral points** : At the neutral point, magnetic field due to the bar magnet is just equal and opposite to the horizontal component of earth's magnetic field.

## Magnetism and Matter

### (i) Magnet is placed horizontally in a horizontal plane.

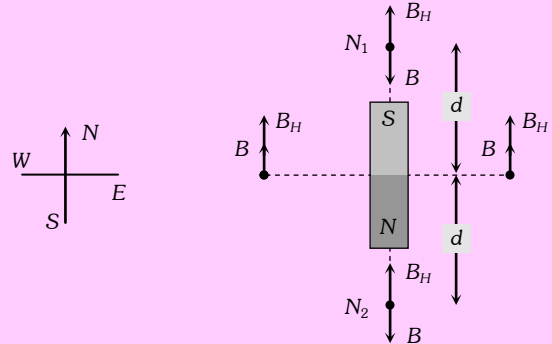
N- pole of magnet is facing N- pole of earth



Two neutral points  $N_1$  and  $N_2$  are obtained on equatorial line of bar magnet as shown and at Neutral points

$$B = B_H \Rightarrow \frac{\mu_0 M}{4\pi d^3} = B_H$$

N - pole of magnet is facing N- pole of earth

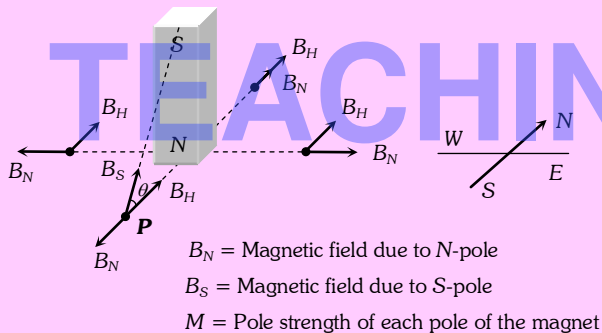


Two neutral points  $N_1$  and  $N_2$  are obtained on axial line of  $B$  or magnet and at neutral points  $B = B_H$  i.e.

$$\frac{\mu_0 \cdot 2M}{4\pi \cdot d^3} = B_H$$

### (ii) Magnet is placed vertically in a horizontal plane

N- pole of magnet is the horizontal plane

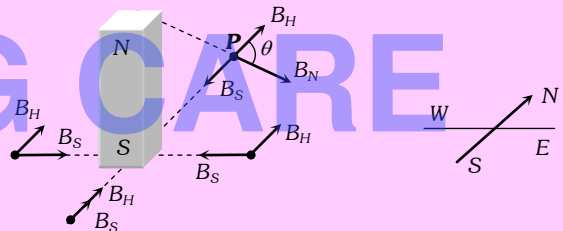


At neutral point  $P$  :  $B_N - B_S \cos\theta = B_H$  ( $B_S < B_N$ )

If suppose effect of S-pole is neglected : As seen from top only one neutral point is obtained as shown and at

$$\text{neutral point } B_N = B_H \Rightarrow \frac{\mu_0 m}{4\pi r^2} = B_H$$

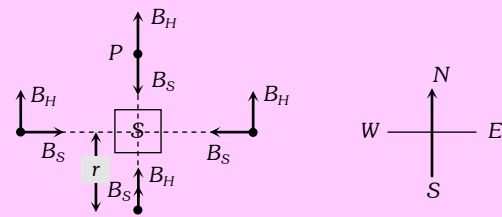
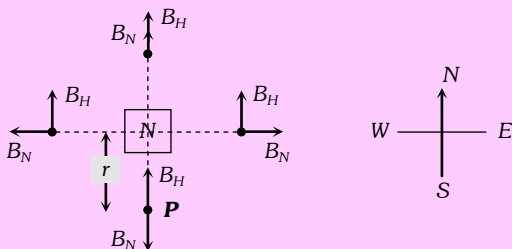
S- pole of magnet is the horizontal plane



At neutral point  $P$  :  $B_S - B_N \cos\theta = B_H$  ( $B_S < B_N$ )

If suppose effect of N-pole is neglected : As seen from top only one neutral point is obtained as shown and at

$$\text{neutral point } B_S = B_H \Rightarrow \frac{\mu_0 m}{4\pi r^2} = B_H$$



### Concepts

- **Apparent dip** : In a vertical plane inclined at an angle  $\beta$  to the magnetic meridian, vertical component of earth's magnetic field

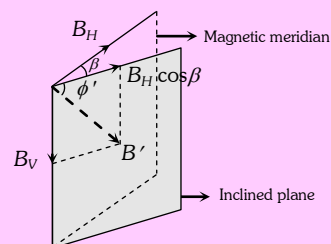
## Magnetism and Matter

remains unchanged while in the new inclined plane horizontal component  $B'_H = B_H \cos \beta$

$\phi'$  = apparent angle of dip

$$\text{and } \tan \phi' = \frac{B_V}{B'_H} = \frac{B_V}{B_H \cos \beta}$$

$$\Rightarrow \tan \phi' = \frac{\tan \phi}{\cos \beta}$$



● If at any place the angle of dip is  $\theta$  and magnetic latitude is  $\lambda$  then  $\tan \theta = 2 \tan \lambda$

● At the poles and equator of earth the values of total intensity are 0.66 and 0.33 Oersted respectively.

### Example

**Example: 19** If the angles of dip at two places are  $30^\circ$  and  $45^\circ$  respectively, Then the ratio of horizontal components of earth's magnetic field at the two places will be [MP PET 1989]

- (a)  $\sqrt{3}:\sqrt{2}$                       (b)  $1:\sqrt{2}$                       (c)  $1:\sqrt{3}$                       (d)  $1:2$

**Solution :** (a) By using  $B_H = B \cos \phi \Rightarrow \frac{(B_H)_1}{(B_H)_2} = \frac{(\cos \phi)_1}{(\cos \phi)_2} = \frac{\cos 30}{\cos 45} = \sqrt{\frac{3}{2}}$

**Example: 20** At a place the earth's horizontal component of magnetic field is  $0.38 \times 10^{-4}$  weber/m<sup>2</sup>. If the angle of dip at that place is  $60^\circ$ , then the vertical component of earth's field at that place in weber/m<sup>2</sup> will be approximately [MP PMT 1985]

- (a)  $0.12 \times 10^{-4}$                       (b)  $0.24 \times 10^{-4}$                       (c)  $0.40 \times 10^{-4}$                       (d)  $0.62 \times 10^{-4}$

**Solution :** (d) By using  $\tan \phi = \frac{B_V}{B_H} \Rightarrow \tan 60^\circ = \frac{B_V}{0.38 \times 10^{-4}} \Rightarrow B_V = 0.38 \times 10^{-4} \times \sqrt{3} = 0.62 \times 10^{-4}$ .

**Example: 21** A dip circle is so set that it moves freely in the magnetic meridian. In this position, the angle of dip is  $40^\circ$ . Now the dip circle is rotated so that the plane in which the needle moves makes an angle of  $30^\circ$  with the magnetic meridian. In this position, the needle will dip by the angle [Roorkee 1983]

- (a)  $40^\circ$                       (b)  $30^\circ$                       (c) More than  $40^\circ$                       (d) Less than  $40^\circ$

**Solution :** (c) By using  $\tan \phi' = \frac{\tan \phi}{\cos \beta}$ ; where  $\phi = 40^\circ$ ,  $\beta = 30^\circ$

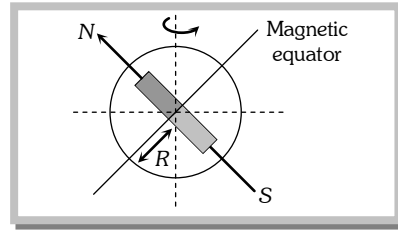
$$\text{As } \cos 30^\circ < 1 \Rightarrow \frac{1}{\cos 30^\circ} > 1$$

$$\text{Hence } \frac{\tan \phi'}{\tan \phi} > 1 \Rightarrow \tan \phi' > \tan \phi = \phi' > \phi \text{ or } \phi' > 40^\circ.$$

**Example: 22** Earth's magnetic field may be supposed to be due to a small bar magnet located at the centre of the earth. If the magnetic field at a point on the magnetic equator is  $0.3 \times 10^{-4}$  T. Magnet moment of bar magnet is

## Magnetism and Matter

- (a)  $7.8 \times 10^8 \text{ amp} \times \text{m}^2$
- (b)  $7.8 \times 10^{22} \text{ amp} \times \text{m}^2$
- (c)  $6.4 \times 10^{22} \text{ amp} \times \text{m}^2$
- (d) None of these

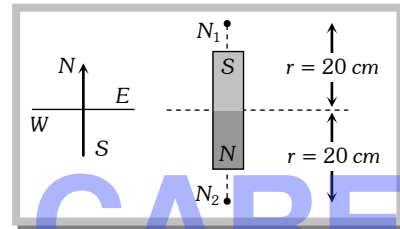


**Solution :** (b) When a magnet is freely suspended in earth's magnetic field, its north pole points north, so the magnetic field of the earth may be suppose to be due to a magnetic dipole with its south pole towards north and as equatorial point is on the broad side on position of the dipole.

$$B_e = \frac{\mu_0}{4\pi} \cdot \frac{M}{r^3} \Rightarrow 0.3 \times 10^{-4} = 10^{-7} \times \frac{M}{(6.4 \times 10^6)^3} \Rightarrow M = 7.8 \times 10^{22} \text{ A-m}^2.$$

**Example: 23** A short bar magnet is placed with its south pole towards geographical north. The neutral points are situated at a distance of 20 cm from the centre of the magnet. If  $B_H = 0.3 \times 10^{-4} \text{ wb/m}^2$  then the magnetic moment of the magnet is

- (a)  $9000 \text{ ab- amp} \times \text{cm}^2$
- (b)  $900 \text{ ab- amp} \times \text{cm}^2$
- (c)  $1200 \text{ ab- amp} \times \text{cm}^2$
- (d)  $225 \text{ ab- amp} \times \text{cm}^2$

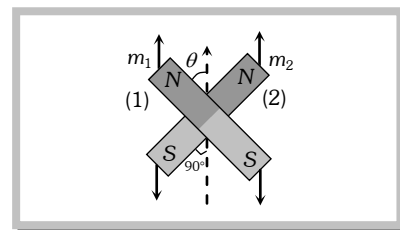


**Solution :** (c) At neutral point magnetic field due to magnet = Horizontal component of earth's magnetic field

$$\Rightarrow \frac{\mu_0}{4\pi} \cdot \frac{2M}{r^3} = B_H \Rightarrow \frac{10^{-7} \times 2 \times M \times 1}{(0.2)^3} = 0.3 \times 15^4 \Rightarrow M = 1.2 \text{ amp} \times \text{m}^2 = 1200 \text{ ab- amp} \times \text{cm}^2.$$

**Example: 24** Two magnets of equal mass are joined at right angles to each other as shown the magnet 1 has a magnetic moment 3 times that of magnet 2. This arrangement is pivoted so that it is free to rotate in the horizontal plane. In equilibrium what angle will the magnet 1 subtend with the magnetic meridian

- (a)  $\tan^{-1}\left(\frac{1}{2}\right)$
- (b)  $\tan^{-1}\left(\frac{1}{3}\right)$
- (c)  $\tan^{-1}(1)$
- (d)  $0^\circ$



**Solution :** (b) For equilibrium of the system torques on  $M_1$  and  $M_2$  due to  $B_H$  must counter balance each other i.e.  $\vec{M}_1 \times \vec{B}_H = \vec{M}_2 \times \vec{B}_H$ . If  $\theta$  is the angle between  $M_1$  and  $B_H$  then the angle between  $M_2$  and  $B_H$  will be  $(90 - \theta)$ ; so  $M_1 B_H \sin \theta = M_2 B_H \sin(90 - \theta)$

$$\Rightarrow \tan \theta = \frac{M_2}{M_1} = \frac{M}{3M} = \frac{1}{3} \Rightarrow \theta = \tan^{-1}\left(\frac{1}{3}\right)$$

## Magnetism and Matter

### Tricky Example: 2

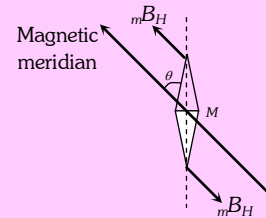
A compass needle whose magnetic moment is  $60 \text{ amp} \times \text{m}^2$  pointing geographical north at a certain place, where the horizontal component of earth's magnetic field is  $40 \mu\text{wb/m}^2$ , experiences a torque  $1.2 \times 10^{-3} \text{ N} \times \text{m}$ . What is the declination at this place [EAMCET (Engg.) 1996]

- (a)  $30^\circ$                       (b)  $45^\circ$                       (c)  $60^\circ$                       (d)  $25^\circ$

**Solution :** (a) As the compass needle is free to rotate in a horizontal plane and points along the magnetic meridian, so when it is pointing along the geographic meridian, it will experience a torque due to the horizontal component of earth's magnetic field i.e.  $\tau = MB_H \sin \theta$

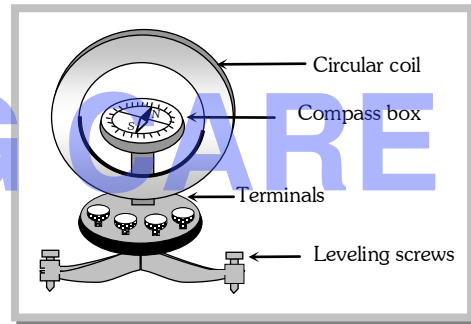
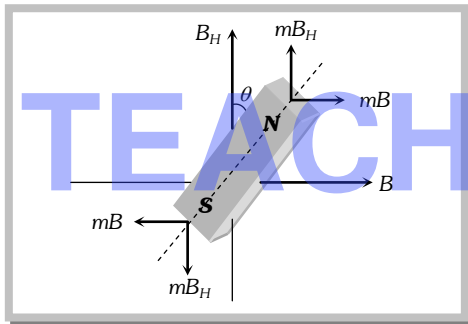
Where  $\theta$  = angle between geographical and magnetic meridians called angle of declination

$$\text{So, } \sin \theta = \frac{1.2 \times 10^{-3}}{60 \times 40 \times 10^{-6}} = \frac{1}{2} \Rightarrow \theta = 30^\circ$$



### Tangent Law and it's Application.

When a small magnet is suspended in two uniform magnetic fields  $B$  and  $B_H$  which are at right angles to each other, the magnet comes to rest at an angle  $\theta$  with respect to  $B_H$  such that  $B = B_H \tan \theta$ . This is called tangent law.



**Tangent galvanometer :** It is an instrument which can detect/measure very small electric currents. It is also called as moving magnet galvanometer. It consists of three circular coils of insulated copper wire wound on a vertical circular frame made of nonmagnetic material as ebonite or wood. A small magnetic compass needle is pivoted at the centre of the vertical circular frame. This needle rotates freely in a horizontal plane inside a box made of nonmagnetic material. When the coil of the tangent galvanometer is kept in magnetic meridian and current passes through any of the coil then the needle at the centre gets deflected and comes to an equilibrium position under the action of two perpendicular field : one due to horizontal component of earth and the other due to field set up by the coil due to current ( $B$ ).

In equilibrium  $B = B_H \tan \theta$  where  $B = \frac{\mu_0 ni}{2r}$ ;  $n$  = number of turns,  $r$  = radius of coil,  $i$  = the current to be measured,  $\theta$  = angle made by needle from the direction of  $B_H$  in equilibrium.

$$\text{Hence } \frac{\mu_0 Ni}{2r} = B_H \tan \theta \Rightarrow i = k \tan \theta \text{ where } k = \frac{2rB_H}{\mu_0 N} \text{ is called reduction factor.}$$

**Note :**  $\cong$  Principle of moving coil galvanometer is  $i \propto \tan \theta$ . Since  $i \propto \tan \theta$  so it's scale is not uniform.

$\cong$  When  $\theta = 45^\circ$ , reduction factor equals to current flows through coil.

$\cong$  Sensitivity of this galvanometer is maximum at  $\theta = 45^\circ$ .

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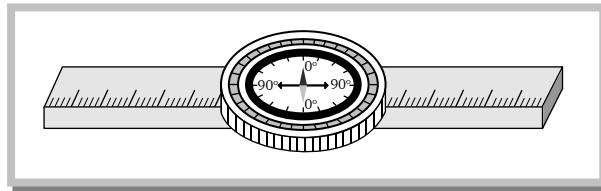
≅ This instrument is also called moving magnet type galvanometer.

### Magnetic Instruments.

Magnetic instruments are used to find out the magnetic moment of a bar magnet, find out the horizontal component of earth's magnetic field, compare the magnetic moments of two bar magnets.

#### (1) Deflection magnetometer

Its working is based on the principle of tangent law. It consists of a small compass needle, pivoted at the centre of a circular box. The box is kept in a wooden frame having two meter scale fitted on its two arms. Reading of a scale at any point directly gives the distance of that point from the centre of compass needle.



Different positions of deflection magnetometer : Deflection magnetometer can be used according to two following positions.

Tan A position	Tan B position
<p>Arms of magnetometer are placed along E-W direction such that magnetic needle is acted upon by only horizontal component of earth's magnetic field (<math>B_H</math>) as shown</p> <p>It a bar magnet is placed on one arm with its length parallel to arm, so magnetic needle comes under the influence of two mutual perpendicular magnetic field (i) <math>B_H</math> and (ii) Axial magnetic field of experimental bar magnet.</p> <p>In equilibrium <math>B = B_H \tan \theta \Rightarrow \frac{\mu_0}{4\pi} \frac{2M}{r^3} = B_H \tan \theta</math></p> <p>(M= Magnetic moment of experimental bar magnet)</p>	<p>Arms of magnetometer are placed along N-S direction such that magnetic needle align itself in the direction of earth's magnetic field (i.e. <math>B_H</math>) as shown.</p> <p>If a bar magnet is placed on one arm with its length perpendicular to arm, so magnetic needle comes under the influence of two mutual perpendicular magnetic fields (i) <math>B_H</math> and (ii) equatorial magnetic field of experimental bar magnet.</p> <p>In equilibrium <math>B = B_H</math> and <math>\Rightarrow \frac{\mu_0}{4\pi} \cdot \frac{M}{r^3} = B_H \tan \theta</math></p>



## Magnetism and Matter

**Note** : ≡ Deflection magnetometer also used to compare the magnetic moments either by deflection method or by null

deflection method. **Deflection method** :  $\frac{M_1}{M_2} = \frac{\tan \theta_1}{\tan \theta_2}$ , **Null deflection method** :  $\frac{M_1}{M_2} = \left(\frac{d_1}{d_2}\right)^3$

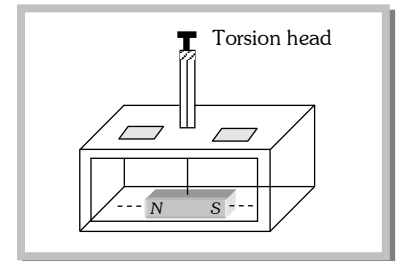
where  $d_1$  and  $d_2$  are the position of two bar magnet placed simultaneously on each arm.

### (2) Vibration magnetometer

Vibration magnetometer is used for comparison of magnetic moments and magnetic fields. This device works on the principle, that whenever a freely suspended magnet in a uniform magnetic field, is disturbed from its equilibrium position, it starts vibrating about the mean position.

Time period of oscillation of experimental bar magnet (magnetic moment  $M$ ) in earth's magnetic field ( $B_H$ ) is given by the formula.  $T = 2\pi \sqrt{\frac{I}{MB_H}}$

Where,  $I$  = moment of inertia of short bar magnet =  $\frac{wL^2}{12}$  ( $w$  = mass of bar magnet)



### (3) Use of vibration magnetometer

(i) Determination of magnetic moment of a magnet :

The experimental (given) magnet is put into vibration magnetometer and its time period  $T$  is determined. Now

$$T = 2\pi \sqrt{\frac{I}{MB_H}} \Rightarrow M = \frac{4\pi^2 I}{B_H \cdot T^2}$$

(ii) Comparison of horizontal components of earth's magnetic field at two places.

$$T = 2\pi \sqrt{\frac{I}{MB_H}} ; \text{ since } I \text{ and } M \text{ the magnet are constant, so } T^2 \propto \frac{1}{B_H} \Rightarrow \frac{(B_H)_1}{(B_H)_2} = \frac{T_2^2}{T_1^2}$$

(iii) Comparison of magnetic moment of two magnets of same size and mass.

$$T = 2\pi \sqrt{\frac{I}{M \cdot B_H}} ; \text{ Here } I \text{ and } B_H \text{ are constants. So } M \propto \frac{1}{T^2} \Rightarrow \frac{M_1}{M_2} = \frac{T_2^2}{T_1^2}$$

(iv) Comparison of magnetic moments of two magnets of unequal sizes and masses (by sum and difference method) :

In this method both the magnets vibrate simultaneously in two following position.

**Sum position** : Two magnets are placed such that their magnetic moments are additive

$$\text{Net magnetic moment } M_s = M_1 + M_2$$

$$\text{Net moment of inertia } I_s = I_1 + I_2$$

Time period of oscillation of this pair in earth's magnetic field ( $B_H$ )

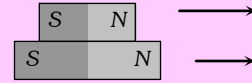
$$T_s = 2\pi \sqrt{\frac{I_s}{M_s B_H}} = 2\pi \sqrt{\frac{I_1 + I_2}{(M_1 + M_2) B_H}} \quad \dots(i)$$

$\vec{M}_1$

$\vec{M}_2$

## Magnetism and Matter

Frequency  $\nu_s = \frac{1}{2\pi} \sqrt{\frac{M_s(B_H)}{I_s}}$

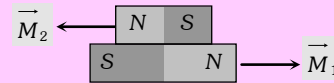


**Difference position :** Magnetic moments are subtractive

Net magnetic moment  $M_d = M_1 + M_2$

Net moment of inertia  $I_d = I_1 + I_2$

and  $T_d = 2\pi \sqrt{\frac{I_d}{M_d B_H}} = 2\pi \sqrt{\frac{I_1 + I_2}{(M_1 - M_2) B_H}}$  .....(ii)



and  $\nu_d = \frac{1}{2\pi} \sqrt{\frac{(M_1 + M_2) B_H}{(I_1 + I_2)}}$

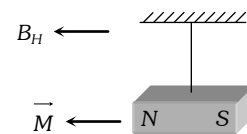
From equation (i) and (ii) we get  $\frac{T_s}{T_d} = \sqrt{\frac{M_1 - M_2}{M_1 + M_2}} \Rightarrow \frac{M_1}{M_2} = \frac{T_d^2 + T_s^2}{T_d^2 - T_s^2} = \frac{\nu_s^2 + \nu_d^2}{\nu_s^2 - \nu_d^2}$

(v) To find the ratio of magnetic field : Suppose it is required to find the ratio  $\frac{B}{B_H}$  where  $B$  is the field created by magnet and  $B_H$  is the horizontal component of earth's magnetic field.

To determine  $\frac{B}{B_H}$  a primary (main) magnet is made to first oscillate in earth's magnetic field ( $B_H$ ) alone and its time period of oscillation ( $T$ ) is noted.

$$T = 2\pi \sqrt{\frac{I}{M B_H}}$$

and frequency  $\nu = \frac{1}{2\pi} \sqrt{\frac{M B_H}{I}}$



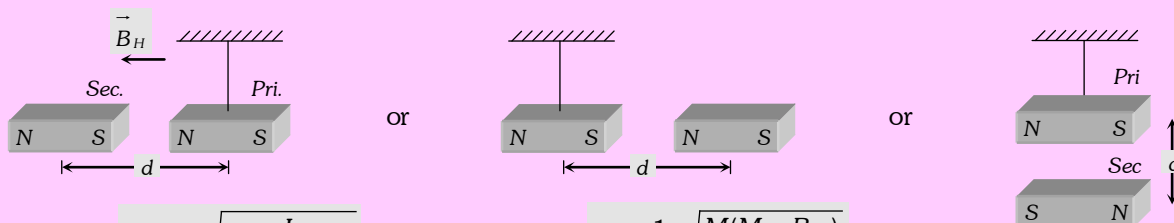
Now a secondary magnet placed near the primary magnet so primary magnet oscillate in a new field with is the resultant of  $B$  and  $B_H$  and now time period, is noted again.

There are two important possibilities for placing secondary magnet

## Magnetism and Matter

### Possibility 1

New field increases so time period of oscillation of primary magnet decreases

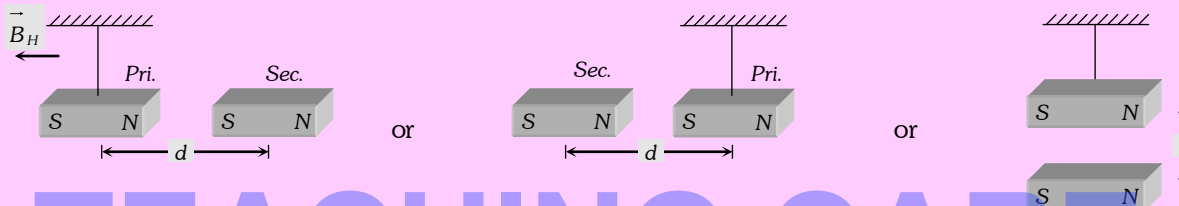


Now time period  $T' = 2\pi \sqrt{\frac{I}{M(B+B_H)}}$  or new frequency  $\nu' = \frac{1}{2\pi} \sqrt{\frac{M(M+B_H)}{I}}$

Also  $\left(\frac{\nu'}{\nu}\right)^2 = \frac{B+B_H}{B_H} \Rightarrow \left(\frac{\nu'}{\nu}\right)^2 = \frac{B}{B_1} + 1 \Rightarrow \frac{B}{B_H} = \left(\frac{\nu'}{\nu}\right)^2 - 1$

### Possibility 2

Net field decreases so time period of oscillation of primary magnet increases



$T' = 2\pi \sqrt{\frac{I}{M(B_H - B)}}$  ( $B_H > B$ ) and  $\nu' = \frac{1}{2\pi} \sqrt{\frac{M(B_H - B)}{I}}$

Also  $\left(\frac{\nu'}{\nu}\right)^2 = \frac{B_H - B}{B_H} \Rightarrow \left(\frac{\nu'}{\nu}\right)^2 = 1 - \left(\frac{B}{B_1}\right) \Rightarrow \frac{B}{B_H} = 1 - \left(\frac{\nu'}{\nu}\right)^2$

### Concepts

- Remember time period of oscillation in difference position is greater than that in sum position  $T_d > T_s$ .
- If a rectangular bar magnet is cut in  $n$  equal parts then time period of each part will be  $\frac{1}{\sqrt{n}}$  times that of complete magnet (i.e.  $T' = \frac{T}{\sqrt{n}}$ ) while for short magnet  $T' = \frac{T}{n}$ . If nothing is said then bar magnet is treated as short magnet.
- Suppose a magnetic needle is vibrating in earth's magnetic field. With temperature rise  $M$  decreases hence time period ( $T$ ) increases but at  $770^\circ\text{C}$  (Curie temperature) it stops vibrating.

### Example

**Example: 25** Two magnets are held together in a vibration magnetometer and are allowed to oscillate in the earth's magnetic field. With like poles together 12 oscillations per minute are made but for unlike poles together only 4 oscillations per minute are executed. The ratio of their magnetic moments is [MP PMT 1996]

- (a) 3 : 1                      (b) 1 : 3                      (c) 3 : 5                      (d) 5 : 4

## Magnetism and Matter

**Solution :** (d) By using  $\frac{M_1}{M_2} = \frac{T_d^2 + T_s^2}{T_d^2 - T_s^2}$ ; where  $T_s = \frac{60}{12} = 5\text{sec}$  and  $T_d = \frac{60}{4} = 15\text{sec}$   $\therefore \frac{M_1}{M_2} = \frac{(15)^2 + (5)^2}{(15)^2 - (5)^2} = \frac{5}{4}$

**Example: 26** The magnetic needle of a tangent galvanometer is deflected at an angle  $30^\circ$  due to a magnet. The horizontal component of earth's magnetic field  $0.34 \times 10^{-4} T$  is along the plane of the coil. The magnetic intensity is

[KCET 1999; AFMC 1999, 2000; BHU 2000; AIIMS 2000, 02]

- (a)  $1.96 \times 10^{-4} T$       (b)  $1.96 \times 10^{-5} T$       (c)  $1.96 \times 10^4 T$       (d)  $1.96 \times 10^5 T$

**Solution :** (b)  $B = B_H \tan \theta \Rightarrow B = 0.34 \times 10^{-4} \tan 30^\circ = 1.96 \times 10^{-5} T$

**Example: 27** A magnet freely suspended in a vibration magnetometer makes 10 oscillations per minute at a place A and 40 oscillations per minute at a place B. If the horizontal component of earth's magnetic field at A is  $36 \times 10^{-6} T$ , then its value at B is

[IIT JEE 2001]

- (a)  $36 \times 10^{-6} T$       (b)  $72 \times 10^{-6} T$       (c)  $144 \times 10^{-6} T$       (d)  $288 \times 10^{-6} T$

**Solution :** (c) By using  $T = 2\pi \sqrt{\frac{I}{MB_H}} \Rightarrow T \propto \frac{1}{\sqrt{B_H}} \Rightarrow \frac{T_A}{T_B} = \sqrt{\frac{(B_H)_B}{(B_H)_A}} \Rightarrow \frac{60/10}{60/20} = \sqrt{\frac{(B_H)_B}{36 \times 10^{-6}}} \Rightarrow (B_H)_B = 144 \times 10^{-6} T$ .

**Example: 28** The magnet of a vibration magnetometer is heated so as to reduce its magnetic moment by 19%. By doing this the periodic time of the magnetometer will

[MP PMT 2000]

- (a) Increase by 19%      (b) Increase by 11%      (c) Decrease by 19%      (d) Decrease by 21%

**Solution :** (b)  $T = 2\pi \sqrt{\frac{I}{MB_H}} \Rightarrow T \propto \frac{1}{\sqrt{M}} \Rightarrow \frac{T_1}{T_2} = \sqrt{\frac{M_2}{M_1}}$   
 If  $M_1 = 100$  then  $M_2 = (100 - 19) = 81$ . So,  $\frac{T_1}{T_2} = \sqrt{\frac{81}{100}} = \frac{9}{10} \Rightarrow T_2 = \frac{10}{9} T_1 = 11\% T_1$

**Example: 29** A magnet makes 40 oscillations per minute at a place having magnetic field intensity  $B_H = 0.1 \times 10^{-5}$ . At another place, it takes 2.5 sec to complete one-vibration. The value of earth's horizontal field at that place

[CPMT 1999; AIIMS 2000]

- (a)  $0.25 \times 10^{-6} T$       (b)  $0.36 \times 10^{-6} T$       (c)  $0.66 \times 10^{-8} T$       (d)  $1.2 \times 10^{-6} T$

**Solution :** (b) By using  $T = 2\pi \sqrt{\frac{I}{MB_H}} \Rightarrow \frac{T_1}{T_2} = \sqrt{\frac{(B_H)_2}{(B_H)_1}} \Rightarrow \frac{60/40}{2.5} = \sqrt{\frac{(B_H)_2}{0.1 \times 10^{-5}}} \Rightarrow (B_H)_2 = 0.36 \times 10^{-6} T$ .

**Example: 30** When 2 amp. current is passed through a tangent galvanometer, it gives a deflection of  $30^\circ$ . For  $60^\circ$  deflection, The current must be

[MP PET 2000]

- (a) 1 amp.      (b)  $2\sqrt{3}$  amp.      (c) 4 amp.      (d) 6 amp.

**Solution :** (d) By using  $i \propto \tan \theta \Rightarrow \frac{i_1}{i_2} = \frac{\tan \theta_1}{\tan \theta_2} \Rightarrow \frac{2}{i_2} = \frac{\tan 30^\circ}{\tan 60^\circ} = \frac{1}{3} \Rightarrow i_2 = 6 \text{ amp.}$

**Example: 31** In vibration magnetometer the time period of suspended bar magnet can be reduced by

[CBSE PMT 1999]

- (a) Moving it towards south pole      (b) Moving it towards north pole  
 (c) Moving it toward equator      (d) Any one them

**Solution :** (c) As we move towards equator  $B_H$  increases and it becomes maximum at equator. Hence  $T = 2\pi \sqrt{\frac{I}{MB_H}}$ , we can say that according to the relation  $T$  decreases as  $B_H \uparrow$  increases (i.e. as we move towards equator).

## Magnetism and Matter

**Example: 32** The time period of a freely suspended magnet is 2 sec. If it is broken in length into two equal parts and one part is suspended in the same way, then its time period will be [MP PMT 1999]

- (a) 4 sec                      (b) 2 sec                      (c)  $\sqrt{2}$  sec                      (d) 1 sec

**Solution :** (d)  $T = 2\pi\sqrt{\frac{I}{MB_H}}$ ; When a bar magnet is broken in  $n$  equal parts so magnetic moment of each part become  $\frac{1}{n}$  times

and moment of inertia becomes of each part becomes  $\frac{1}{n^3}$  times. Hence time period becomes  $\frac{1}{n}$  times i.e.  $T' = \frac{T}{4}$

In this question  $n = 2$  so,  $T' = \frac{T}{2} = \frac{2}{2} = 1\text{sec}$

**Example: 33** A magnet is suspended in such a way that it oscillates in the horizontal plane. It makes 20 oscillations per minute at a place where dip angle is  $30^\circ$  and 15 oscillations per minute at a place where dip angle is  $60^\circ$ . The ratio of total earth's magnetic field at the two places is [MP PMT 1991; BHU 1997]

- (a)  $3\sqrt{3}:8$                       (b)  $16:9\sqrt{3}$                       (c)  $4:9$                       (d)  $2\sqrt{3}:9$

**Solution :** (b) By using  $T = 2\pi\sqrt{\frac{I}{MB_H}} = 2\pi\sqrt{\frac{I}{MB\cos\phi}}$

$$\Rightarrow T \propto \frac{1}{\sqrt{B\cos\phi}} \Rightarrow \frac{T_1}{T_2} = \sqrt{\frac{B_2 \times \cos\phi_2}{B_1 \times \cos\phi_1}} \Rightarrow \frac{60/20}{60/15} = \sqrt{\frac{B_2 \times \cos 60^\circ}{B_1 \times \cos 30^\circ}} \Rightarrow \frac{B_1}{B_2} = \frac{16}{9\sqrt{3}}$$

**Example: 34** If  $\theta_1$  and  $\theta_2$  are the deflections obtained by placing small magnet on the arm of a deflection magnetometer at the same distance from the compass box in tan A and tan B positions of the magnetometer respectively then the value of  $\frac{\tan\theta_1}{\tan\theta_2}$  will be approximately [MP PMT 1992]

- (a) 1                      (b) 2                      (c)  $\frac{1}{2}$                       (d)  $\sqrt{2}$

**Solution :** (b) In tan A position  $\frac{\mu_0}{4\pi} \cdot \frac{2M}{d^3} = B_H \tan\theta_1$  .....(i)

In tan B position  $\frac{\mu_0}{4\pi} \cdot \frac{M}{d^3} = B_H \tan\theta_2$  .....(ii)

Dividing equation (i) by equation (ii)  $\frac{\tan\theta_1}{\tan\theta_2} = \frac{2}{1}$ .

**Example: 35** In a vibration magnetometer, the time period of a bar magnet oscillating in horizontal component of earth's magnetic field is 2 sec. When a magnet is brought near and parallel to it, the time period reduces to 1 sec. The ratio  $H/F$  of the horizontal component  $H$  and the field  $F$  due to magnet will be [MP PMT 1990]

- (a) 3                      (b)  $\frac{1}{3}$                       (c)  $\sqrt{3}$                       (d)  $\frac{1}{\sqrt{3}}$

**Solution :** (b) Time period decreases i.e. field due to magnet ( $F$ ) assist the horizontal component of earth's magnetic field (see theory)

## Magnetism and Matter

Hence by using  $\frac{B}{B_H} = \left(\frac{T}{T'}\right)^2 - 1 \Rightarrow \frac{F}{H} = \left(\frac{2}{1}\right)^2 - 1 = 3 \Rightarrow \frac{H}{F} = \frac{1}{3}$ .

- Example: 36** A certain amount of current when flowing in a properly set tangent galvanometer, produces a deflection of  $45^\circ$ . If the current be reduced by a factor of  $\sqrt{3}$ , the deflection would
- (a) Decrease by  $30^\circ$       (b) Decreases by  $15^\circ$       (c) Increase by  $15^\circ$       (d) Increase by  $30^\circ$

**Solution :** (b) By using  $i \propto \tan \theta \Rightarrow \frac{i_1}{i_2} = \frac{\tan \theta_1}{\tan \theta_2} \Rightarrow \frac{i_1}{i_1/\sqrt{3}} = \frac{\tan 45^\circ}{\tan \theta_2} \Rightarrow \sqrt{3} \tan \theta_2 = 1 \Rightarrow \tan \theta_2 = \frac{1}{\sqrt{3}} \Rightarrow \theta_2 = 30^\circ$

So deflection will decrease by  $45^\circ - 30^\circ = 15^\circ$ .

- Example: 37** The angle of dip at a place is  $60^\circ$ . A magnetic needle oscillates in a horizontal plane at this place with period  $T$ . The same needle will oscillate in a vertical plane coinciding with the magnetic meridian with a period

- (a)  $T$       (b)  $2T$       (c)  $\frac{T}{2}$       (d)  $\frac{T}{\sqrt{2}}$

**Solution :** (d) When needle oscillates in horizontal plane

Then it's time period is  $T = 2\pi \sqrt{\frac{I}{MB_H}}$  .....(i)

When needle oscillates in vertical plane i.e. It oscillates in total earth's total magnetic field (B)

Hence  $T' = 2\pi \sqrt{\frac{I}{MB}}$  .....(ii)

Dividing equation (ii) by (i)  $\frac{T'}{T} = \sqrt{\frac{B_H}{B}} = \sqrt{\frac{B \cos \phi}{B}} = \sqrt{\cos 60} = \frac{1}{\sqrt{2}} \Rightarrow T' = \frac{T}{\sqrt{2}}$

- Example: 38** A dip needle vibrates in the vertical plane perpendicular to the magnetic meridian. The time period of vibration is found to be 2 seconds. The same needle is then allowed to vibrate in the horizontal plane and the time period is again found to be 2 seconds. Then the angle of dip is

- (a)  $0^\circ$       (b)  $30^\circ$       (c)  $45^\circ$       (d)  $90^\circ$

**Solution :** (c) In vertical plane perpendicular to magnetic meridian.

$T = 2\pi \sqrt{\frac{I}{MB_V}}$  .....(i)

In horizontal plane  $T = 2\pi \sqrt{\frac{I}{MB_H}}$  .....(ii)

Equation (i) and (ii) gives  $B_V = B_H$

Hence by using  $\tan \phi = \frac{B_V}{B_H} \Rightarrow \tan \phi = 1 \Rightarrow \phi = 45^\circ$

## Magnetism and Matter

### Tricky Example: 3

A magnet is suspended horizontally in the earth's magnetic field. When it is displaced and then released it oscillates in a horizontal plane with a period  $T$ . If a piece of wood of the same moment of inertia (about the axis of rotation) as the magnet is attached to the magnet what would the new period of oscillation of the system become

- (a)  $\frac{T}{3}$                       (b)  $\frac{T}{2}$                       (c)  $\frac{T}{\sqrt{2}}$                       (d)  $T\sqrt{2}$

**Solution :** (d) Due to wood moment of inertia of the system becomes twice but there is no change magnetic moment of the system.

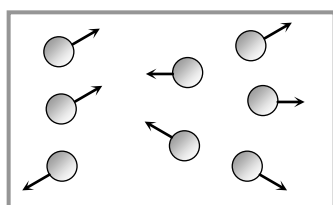
$$\text{Hence by using } T = 2\pi \sqrt{\frac{I}{MB_H}} \Rightarrow T \propto \sqrt{I} \Rightarrow T' = \sqrt{2} T$$

### Magnetic Materials.

(1) **Types of magnetic material :** On the basis of mutual interactions or behaviour of various materials in an external magnetic field, the materials are divided in three main categories.

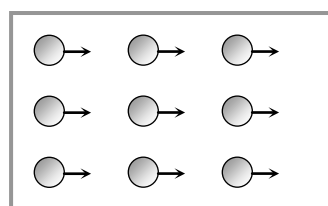
(i) **Diamagnetic materials :** Diamagnetism is the intrinsic property of every material and it is generated due to mutual interaction between the applied magnetic field and orbital motion of electrons.

(ii) **Paramagnetic materials :** In these substances the inner orbits of atoms are incomplete. The electron spins are uncoupled, consequently on applying a magnetic field the magnetic moment generated due to spin motion align in the direction of magnetic field and induces magnetic moment in its direction due to which the material gets feebly magnetised. In these materials the electron number is odd.



(a)

When no field is applied



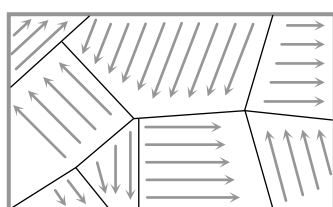
(b)

On application of field (B)

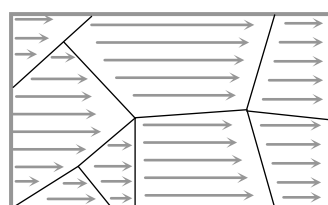
(iii) **Ferromagnetic materials :** In some materials, the permanent atomic magnetic moments have strong tendency to align themselves even without any external field.

These materials are called ferromagnetic materials.

In every unmagnetised ferromagnetic material, the atoms form domains inside the material. The atoms in any domain have magnetic moments in the same direction giving a net large magnetic moment to the domain. Different domains, however, have different directions of magnetic moment and hence the materials remain unmagnetised. On applying an external magnetic field, these domains rotate and align in the direction of magnetic field.



Unmagnetised



Magnetised

## Magnetism and Matter

(2) **Curie Law** : The magnetic susceptibility of paramagnetic substances is inversely proportional to its absolute temperature i.e.  $\chi \propto \frac{1}{T} \Rightarrow \chi \propto \frac{C}{T}$

where  $C$  = Curie constant,  $T$  = absolute temperature

On increasing temperature, the magnetic susceptibility of paramagnetic materials decreases and vice versa.

The magnetic susceptibility of ferromagnetic substances does not change according to Curie law.

(i) Curie temperature ( $T_c$ ) : The temperature above which a ferromagnetic material behaves like a paramagnetic material is defined as Curie temperature ( $T_c$ ).

or

The minimum temperature at which a ferromagnetic substance is converted into paramagnetic substance is defined as Curie temperature.

For various ferromagnetic materials its values are different, e.g. for Ni,  $T_{C_{Ni}} = 358^\circ C$

for Fe,  $T_{C_{Fe}} = 770^\circ C$

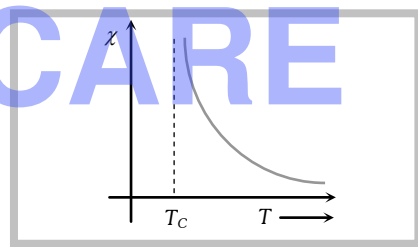
for CO,  $T_{C_{CO}} = 1120^\circ C$

At this temperature the ferromagnetism of the substances suddenly vanishes.

(ii) Curie-weiss law : At temperatures above Curie temperature the magnetic susceptibility of ferromagnetic materials is inversely proportional to  $(T - T_c)$  i.e.  $\chi \propto \frac{1}{T - T_c}$

$$\Rightarrow \chi = \frac{C}{(T - T_c)} \text{ Here } T_c = \text{Curie temperature}$$

$\chi$ - $T$  curve is shown (for Curie-Weiss Law)



### (3) Comparative study of magnetic materials

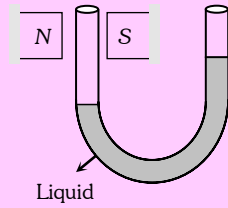
Property	Diamagnetic substances	Paramagnetic substances	Ferromagnetic substances
Cause of magnetism	Orbital motion of electrons	Spin motion of electrons	Formation of domains
Explanation of magnetism	On the basis of orbital motion of electrons	On the basis of spin and orbital motion of electrons	On the basis of domains formed
Behaviour In a non-uniform magnetic field	These are repelled in an external magnetic field i.e. have a tendency to move from high to low field region.	These are feebly attracted in an external magnetic field i.e., have a tendency to move from low to high field region	These are strongly attracted in an external magnetic field i.e. they easily move from low to high field region
State of magnetisation	These are weakly magnetised in a direction opposite to that of applied magnetic field	These get weakly magnetised in the direction of applied magnetic field	These get strongly magnetised in the direction of applied magnetic field
When the material in the	Liquid level in that limb	Liquid level in that limb	Liquid level in that limb



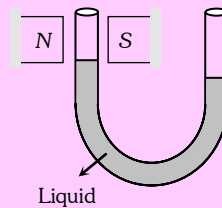
## Magnetism and Matter

form of liquid is filled in the U-tube and placed between pole pieces.

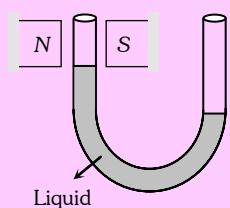
gets depressed



rises up



rises up very much



On placing the gaseous materials between pole pieces

The gas expands at right angles to the magnetic field.

The gas expands in the direction of magnetic field.

The gas rapidly expands in the direction of magnetic field

The value of magnetic induction  $B$

$$B < B_0$$

$$B > B_0$$

$$B \gg B_0$$

where  $B_0$  is the magnetic induction in vacuum

Magnetic susceptibility  $\chi$

Low and negative  $|\chi| \approx 1$

Low but positive  $\chi \approx 1$

Positive and high  $\chi \approx 10^2$

Dependence of  $\chi$  on temperature

Does not depend on temperature (except  $B_i$  at low temperature)

Inversely proportional to temperature  $\chi \propto \frac{1}{T}$  or

$$\chi \propto \frac{1}{T - T_c} \text{ or}$$

$$\chi = \frac{C}{T}. \text{ This is called}$$

$$\chi = \frac{C}{T - T_c} \text{ This is called}$$

Curie law, where  $C =$  Curie constant

Curie Weiss law.

$T_c =$  Curie temperature

Dependence of  $\chi$  on  $H$

Does not depend independent

Does not depend independent

Does not depend independent

Relative permeability ( $\mu_r$ )

$$\mu_r < 1$$

$$\mu_r > 1$$

$$\mu_r \gg 1$$

$$\mu_r = 10^2$$

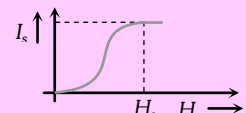
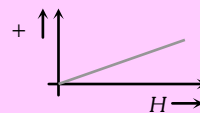
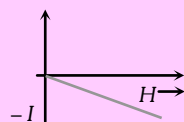
Intensity of magnetisation ( $I$ )

$I$  is in a direction opposite to that of  $H$  and its value is very low

$I$  is in the direction of  $H$  but value is low

$I$  is in the direction of  $H$  and value is very high.

$I$ - $H$  curves



Magnetic moment ( $M$ )

The value of  $M$  is very low ( $\approx 0$  and is in a direction opposite to  $H$ .)

The value of  $M$  is very low and is in the direction of  $H$

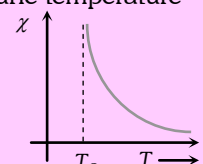
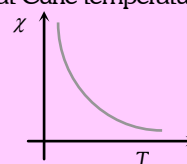
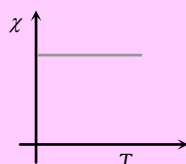
The value of  $M$  is very high and is in the direction of  $H$

Transition of materials (at Curie temperature)

These do not change.

On cooling, these get converted to ferromagnetic materials at Curie temperature

These get converted into paramagnetic materials above Curie temperature

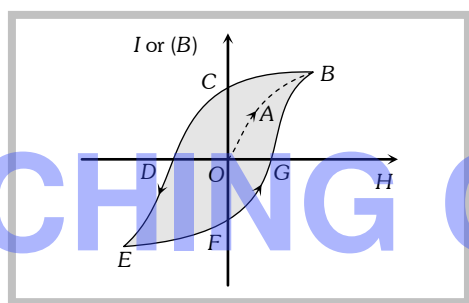


## Magnetism and Matter

The property of magnetism	Diamagnetism is found in those materials the atoms of which have even number electrons	Paramagnetism is found in those materials the atoms of which have majority of electron spins in the same direction	Ferro-magnetism is found in those materials which when placed in an external magnetic field are strongly magnetised
Examples	<i>Cu, Ag, Au, Zn, Bi, Sb, NaCl, H<sub>2</sub>O</i> air and diamond <i>etc.</i>	<i>Al, Mn, Pt, Na, CuCl<sub>2</sub>, O<sub>2</sub></i> and crown glass	<i>Fe, Co, Ni, Cd, Fe<sub>3</sub>O<sub>4</sub></i> <i>etc.</i>
Nature of effect	Distortion effect	Orientation effect	Hysteresis effect

**(4) Hysteresis :** For ferromagnetic materials, by removing external magnetic field *i.e.*  $H = 0$ . The magnetic moment of some domains remain aligned in the applied direction of previous magnetising field which results into a residual magnetism.

The lack of retracibility as shown in figure is called hysteresis and the curve is known as hysteresis loop.



(i) When magnetising field ( $H$ ) is increased from  $O$ , the intensity of magnetisation  $I$  increases and becomes maximum. This maximum value is called the saturation value.

(ii) When  $H$  is reduced,  $I$  reduces but is not zero when  $H = 0$ . The remainder value  $OC$  of magnetisation when  $H = 0$  is called the residual magnetism or retentivity.

The property by virtue of which the magnetism ( $I$ ) remains in a material even on the removal of magnetising field is called Retentivity or Residual magnetism.

(iii) When magnetic field  $H$  is reversed, the magnetisation decreases and for a particular value of  $H$ , denoted by  $H_c$ , it becomes zero *i.e.*,  $H_c = OD$  when  $I = 0$ . This value of  $H$  is called the corecivity.

(iv) So, the process of demagnetising a material completely by applying magnetising field in a negative direction is defined Corecivity. Corecivity assesses the softness or hardness of a magnetic material. Corecivity signifies magnetic hardness or softness of substance :

Magnetic hard substance (steel) → High corecivity

Magnetic soft substance (soft iron) → Low corecivity

(v) When field  $H$  is further increased in reverse direction, the intensity of magnetisation attains saturation value in reverse direction (*i.e.* point  $E$ )

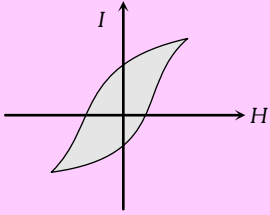
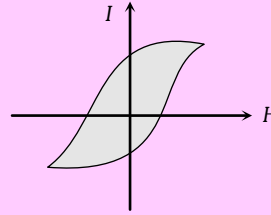
## Magnetism and Matter

(vi) When  $H$  is decreased to zero and changed direction in steps, we get the part  $EFGB$ .

Thus complete cycle of magnetisation and demagnetisation is represented by  $BCDEFGB$ .

**Note** :  $\cong$  The energy loss (or hysteresis energy loss) in magnetising and demagnetising a specimen is proportional to the area of hysteresis loop.

(vii) Comparison between soft iron and steel :

Soft iron	Steel
	
The area of hysteresis loop is less (low energy loss) Less retentivity and coercive force Magnetic permeability is high Magnetic susceptibility ( $\chi$ ) is high Intensity of magnetisation ( $I$ ) is high It magnetised and demagnetised easily Used in dynamo, transformer, electromagnet tape recorder and tapes etc.	The area of hysteresis loop is large (high energy loss) More retentivity and coercive force Magnetic permeability is less $\chi$ is low $I$ is low Magnetisation and demagnetisation is complicated Used for making permanent magnet.

### Concepts

- An iron cored coil and a bulb are connected in series with an ac generator. If an iron rod is introduced inside a coil, then the intensity of bulb will decrease, because some energy lost in magnetising the rod.
- Hysteresis energy loss = Area bound by the hysteresis loop =  $VAn$  Joule
- Where,  $V$  = Volume of ferromagnetic sample,  $A$  = Area of  $B-H$  loop,  $n$  = Frequency of alternating magnetic field and  $t$  = Time.

### Example

**Example: 39** A ferromagnetic substance of volume  $10^{-3} \text{ m}^3$  is placed in an alternating field of 50 Hz. Area of hysteresis curve obtained is 0.1 M.K.S. unit. The heat produced due to energy loss per second in the substance will be  
 (a) 5 J                                      (b)  $5 \times 10^{-2} \text{ cal}$                                       (c)  $1.19 \times 10^{-3} \text{ cal}$                                       (d) No loss of energy

**Solution :** (c) By using heat loss =  $VAn$  ; where  $V$  = volume =  $10^{-3} \text{ m}^3$ ;  $A$  = Area =  $0.1 \text{ m}^2$ ,  $n$  = frequency = 50 Hz and  $t$  = time = 1sec  
 Heat loss =  $10^{-3} \times 0.1 \times 50 \times 1 = 5 \times 10^{-3} \text{ J} = 1.19 \times 10^{-3} \text{ cal}$

**Example: 40** A magnetising field of  $1600 \text{ A-m}^{-1}$  produces a magnetic flux of  $2.4 \times 10^{-5} \text{ Wb}$  in an iron bar of cross-sectional area  $0.2 \text{ cm}^2$ . The susceptibility of an iron bar is [BHU 2002]

## Magnetism and Matter

- (a) 298                                      (b) 596                                      (c) 1192                                      (d) 1788

**Solution :** (b) By using  $B = \mu H = \mu_0 \mu_r H$  and  $\mu_r = (1 + \chi_m) \Rightarrow \mu_r = \frac{B}{\mu_0 H} = \frac{\phi}{\mu_0 HA}$

$$\mu_r = \frac{2.4 \times 10^{-5}}{(4\pi \times 10^{-7}) \times 1600 \times (0.2 \times 10^{-4})} = 596.8. \text{ Hence } \chi_m = 595.8 \approx 596$$

**Example: 41** For iron its density is  $7500 \text{ kg/m}^3$  and mass  $0.075 \text{ kg}$ . If its magnetic moment is  $8 \times 10^{-7} \text{ Amp} \times \text{m}^2$ , its intensity of magnetisation is

- (a)  $8 \text{ Amp/m}$                                       (b)  $0.8 \text{ Amp/m}$                                       (c)  $0.08 \text{ Amp/m}$                                       (d)  $0.008 \text{ Amp/m}$

**Solution :** (c)  $I = \frac{M}{V} = \frac{Md}{m} = \frac{8 \times 10^{-7} \times 7500}{0.075} = 0.08 \text{ Amp/m}$

**Example: 42** The dipole moment of each molecule of a paramagnetic gas is  $1.5 \times 10^{-23} \text{ Amp} \times \text{m}^2$ . The temperature of gas is  $27^\circ\text{C}$  and the number of molecules per unit volume in it is  $2 \times 10^{26} \text{ m}^{-3}$ . The maximum possible intensity of magnetisation in the gas will be

- (a)  $3 \times 10^3 \text{ Amp/m}$                                       (b)  $4 \times 10^3 \text{ Amp/m}$                                       (c)  $5 \times 10^5 \text{ Amp/m}$                                       (d)  $6 \times 10^4 \text{ Amp/m}$

**Solution :** (a)  $I = \frac{M}{V} = \frac{\mu N}{V} = \frac{1.5 \times 10^{-23} \times 2 \times 10^{26}}{1} = 3 \times 10^3 \text{ Amp/m}$

**Example: 43** The coercivity of a small bar magnet is  $4 \times 10^3 \text{ Amp/m}$ . It is inserted inside a solenoid of 500 turns and length  $1 \text{ m}$  to demagnetise it. The amount of current to be passed through the solenoid will be

- (a)  $2.5 \text{ A}$                                       (b)  $5 \text{ A}$                                       (c)  $8 \text{ A}$                                       (d)  $10 \text{ A}$

**Solution :** (c)  $H = ni \Rightarrow i = \frac{H}{n} = \frac{4 \times 10^3}{500} = 8 \text{ A}$

**Example: 44** The units for molar susceptibility

- (a)  $\text{m}^3$                                       (b)  $\text{kg-m}^{-3}$                                       (c)  $\text{kg}^{-1} \text{m}^3$                                       (d) No units

**Solution :** (a) Molar susceptibility =  $\frac{\text{Volume susceptibility}}{\text{Density of material}} \times \text{molecular weight} = \frac{I/H}{\rho} \times M = \frac{I/H}{M/V} \times M$

So its unit is  $\text{m}^3$ .

**Example: 45** The ratio of the area of  $B$ - $H$  curve and  $I$ - $H$  curve of a substance in M.K.S. system is

- (a)  $\mu_0^2$                                       (b)  $\frac{1}{\mu_0^2}$                                       (c)  $\mu_0$                                       (d)  $\frac{1}{\mu_0}$

**Solution :** (c) Area of  $B$ - $H$  loop =  $\mu_0$  (Area of  $I$ - $H$ )